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Control of Asymmetrical Multilevel Inverter Using Artificial Neural Network

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Introduction

Inverters are widely used in modern power grids; a great focus is therefore made in different research fields in order to develop their performance. Three-level inverters are now conventional apparatus but other topologies have been attempted this last decade for different kinds of applications [1]. Among them, Neutral Point Clamped (NPC) inverters, flying capacitors inverters also called imbricated cells, and series connected cells inverters called cascaded inverters [2].

This paper is a study about a three-phase multilevel converter based on series connected single phase inverters (partial cells) in each phase. A multilevel converter with k partial inverters connected in serial is presented by Fig.1. In this configuration, each cell of rank j = 1, ...k is supplied by a dc-voltage source u_{dj} . It has been shown that feeding partial cells with unequal dc-voltages (asymmetric feeding) increases the number of levels of the generated output voltage without any supplemental complexity to the existing topology [3]. These inverters are referred to as "Asymmetrical Multilevel Inverters" or AMI.



Fig.1. Three-phase structure of a multilevel converter with *k* partial monophased inverters series connected per phase

Some applications such as active power filtering need inverters with high performances [4]. These performances are obtained if there are still any harmonics at the output voltages and currents. Different Pulse-Width Modulation (PWM) control-techniques have been proposed in order to reduce the residual harmonics at the output and to increase the performances of the inverters [5]. The most popular one is probably the multi-carrier PWM technique [6] which shifts the harmonics to high frequencies by using high-frequency carriers. However, electronic devices and components have limited switching-frequencies. Highfrequency carriers are therefore limited by this constraint. An alternative solution consists in adapting the principle of the Harmonics Elimination Strategy (HES) to AMIs. The HES allows canceling the critical harmonic distortions and therefore controlling the fundamental component of the signal by using electronic devices with low switching frequencies.

The principle of this technique relies on the resolution of a system of non linear equations to elaborate the switching angle control signals for the electronic devices [7]. Practically, the implementation of this method requires memorizing all the firing angles which is complex and needs considerable computational costs. Mathematical solutions with limited computational costs are therefore preferably used for real-time applications. The approach can be achieved with Artificial Neural Networks (ANNs) which are known as parsimonious universal approximators. Their learning from examples leads to robust generalization capabilities [8].

This paper proposes a HES based on ANNs to control a 9-level Uniform Step Asymmetrical Multilevel Inverter (USAMI). Standard Multi-Layer Perceptrons (MLP) [9] are used for approximating the relationship between the modulation rate and the inverters switching angles. The performance of this neural approach is evaluated and compared to the MCPWM technique. The proposed neural strategy is also evaluated when the inverter supplies an asynchronous machine. In this application, it is important that the implemented controller computes appropriate switching angles for the inverters in order to minimize the harmonics absorbed by the asynchronous machine. Performances where successfully achieved, the neural controller demonstrates a satisfying behavior and a good robustness.

Uniform Step Asymmetrical Multilevel Inverters

Multilevel inverters generate at the ac-terminal several voltage levels as close as possible to the input signal. The output voltage step is defined by the difference between two consecutive voltages. A multilevel converter has a uniform or regular voltage step, if the steps Δu between all voltage levels are equal. In this case the step is equal to the smallest dc-voltage, u_{d1} [6]. This can be expressed by

$$u_{s2} - u_{s1} = u_{s3} - u_{s2} = \dots = u_{sN} - u_{s(N-1)} = \Delta u = u_{d1}, \quad (1)$$

with N voltage levels. If this is not the case, the converter is called a non uniform step AMI or irregular AMI. An USAMI is based on dc-voltage sources to supply the partial cells (inverters) composing its topology which respects to the following conditions [6]

$$\begin{cases} u_{d1} \le u_{d2} \le \dots \le u_{dk}; \\ u_{dj} \le 1 + 2\sum_{l=1}^{j-1} u_{dl}, \end{cases}$$
(2)

where *k* represents the number of partial cells per phase; j = 1, ...k. The number of levels of the output voltage can be deduced from

$$N = 1 + 2\sum_{j=1}^{k} u_{dj} .$$
 (3)

This relationship fundamentally modifies the number of levels generated by the multilevel topology. Indeed, the value of N depends on the number of cells per phase and the corresponding supplying dc-voltages.

Equation (3) accepts different solutions. With k = 3 for example, there are two possible combinations of supply voltages for the partial inverters in order to generate a 11level global output, i.e., $(u_{d1}, u_{d2}, u_{d3}) \in \{(1, 1, 3); (1, 2, u_{d3})\}$ 2)}, and there are three possible combinations to generate a 15-level global output, i.e., $(u_{d1}, u_{d2}, u_{d3}) \in \{(1, 1, 5); (1, 2, 1, 2)\}$ 4); (1, 3, 3). Fig. 2 shows the possible output voltages of the three partial cells of the 9-level inverter with k = 3. The dc-voltages of the three cells are $u_{d1} = 1p.u.$, $u_{d2} = 1p.u.$ and $u_{d3} = 2p.u$. The output voltages of each partial inverter are noted u_{p1} , u_{p2} and u_{p3} and can take three different values: $u_{p1} \in \{-1, 0, 1\}, u_{p2} \in \{-1, 0, 1\}$ and $u_{p3} \in \{-2, 0, 2\}$. The result is a generated output voltage with 9 levels: $u_s \in \{-4, -4\}$ -3, -2, -1, 0, 1, 2, 3, 4. Some levels of the output voltage can be generated by different commutation sequences. For example, there are four possible commutation sequences resulting in $u_s = 2p.u.$: $(u_{p1}, u_{p2}, u_{p3}) \in \{(-1, 1, 2); (0, 0, 2);$ (1, -1, 2); (1, 1, 0). These redundant combinations can be selected in order to optimize the switching process of the inverter [10]. These different possibilities offered by the output voltage of the partial inverters, and the redundancies among them to deliver a same output voltage level, can be considered as degrees of freedom which can be exploited in order to optimize the use of a AMI.



Fig. 2. Possible output voltages of each partial inverter to generate N = 9 levels with k = 3 cells per phase (with $u_{d1} = 1p.u.$, $u_{d2} = 1p.u.$ and $u_{d3} = 2p.u.$)

Multilevel Inverters Control Strategies

Several modulation strategies have been proposed for symmetrical multilevel converters. They are generally derived from the classical modulation techniques used for more traditional converters [10]. Among these methods, the most common used is the multi-carrier sub-harmonic PWM technique. This modulation method can also be used to control asymmetrical multilevel power converters. In the case of AMIs, other kinds of modulation can be used [3].

In this Section, we briefly introduce the MCPWM technique. We also propose a HES based on ANNs. These control strategies will be compared by computer simulations. The objective is to elaborate optimized switching angles for an 9-level USAMI. The inverter is then employed to supply an asynchronous machine.

Multi-Carrier PWM (MCPWM)

The principle of the MCPWM is based on a comparison of a sinusoidal reference waveform with vertically shifted carrier waveforms. N - 1 carriers are required to generate N levels. The carriers are in continuous bands around the reference zero. They have the same amplitude A_c and the same frequency f_c . The sine reference waveform has a frequency f_r and an amplitude A_r . At each instant, the result of the comparison is 1 if the triangular carrier is greater than the reference signal and 0 otherwise. The output of the modulator is the sum of the different comparisons which represents the voltage level. The strategy is therefore characterized by the two following parameters [6], respectively called the modulation index and the modulation rate:

$$n = \frac{f_c}{f_r},\tag{4}$$

$$r = \frac{2}{N-1} \frac{A_r}{A_c} \,. \tag{5}$$

We propose to develop a 9-level inverter composed of k = 3 partial inverters per phase with the following devoltage sources: with *p.u* units: $u_{d1} = 1p.u.$, $u_{d2} = 1p.u.$ and $u_{d3} = 2p.u.$, and with *SI* units: $U_{d1} = 100V$, $U_{d2} = 100V$ and $U_{d3} = 200V$. The output voltage V_{ab} and its frequency

representation are respectively presented by Fig. 3 and Fig. 4.



Fig. 3. Output voltage V_{ab} of the 9-level USAMI controlled by the MCPWM (with m = 24 and r = 0.8)



Fig. 4. Frequency content of the output voltage V_{ab} with the MCPWM strategy (with m = 24 and r = 0.8)

Harmonics Elimination Strategy with ANNs

A) Harmonics Elimination Strategy (HES): The HES is based on the Fourier analysis of the generated voltage u_s at the output of the USAMI [11]. This voltage is symmetric in a half and a quarter of a period. As a result, the even harmonic components are null. The Fourier series expansion for the u_s voltage is thus:

$$\begin{cases} u_s = \sum_{n=1}^{\infty} u_n \sin n \omega t; \\ u_n = \frac{4u_{d1}}{n\pi} \sum_{i=1}^{p} \cos n \theta_i, \end{cases}$$
(6)

where u_n represents the amplitude of the harmonic term of rank n; p = (N - 1)/2 – the number of switching over a quarter of a period,; θ_i – the switching angles (i = 1, 2..., p).

The *p* switching angles in (6) are calculated by fixing the amplitude of the fundamental term and by canceling the p - 1 other harmonic terms. Practically, four switching angles (θ_1 , θ_2 ... θ_4) are necessary for canceling the three first harmonics terms (i.e., harmonics with a odd rank and non multiple of 3, therefore 5, 7 and 11) in the case of a three phase 9-level USAMI composed of k = 3 partial inverters per phase supplied by the dc-voltages $u_{d1} = 1p.u.$, $u_{d2} = 1p.u.$ and $u_{d3} = 2p.u$. These switching angles can be determined by solving the following system of non linear equations

$$\begin{cases} \sum_{i=1}^{4} \cos \theta_i = \pi r; \\ \sum_{i=1}^{4} \cos n \theta_i = 0 \text{ for } n \in \{5, 7, 11\}, \end{cases}$$

$$(7)$$

where $r = u_1/4u_{d1}$ – the modulation rate. The solution of (7) must also satisfy

$$\theta_1 < \theta_2 < \theta_3 < \theta_4 < \frac{\pi}{2}, \tag{8}$$

and can be solved by applying the Newton-Raphson method. This method returns all the possible combinations of the switching angles for different values of r. The result is represented by Fig. 5 where one can see the presence of two possible solutions of angles for $0.70 \le r \le 0.76$. On the other side, the system does not accept any solution for r < 0.629, 0.64 < r < 0.7 and 0.897 < r < 0.921. The system has an unique solution for all the other values of r.

In the case of two possible solutions for an angle θ_i , the criteria for selecting one of them can be the Total Harmonic Distortion (THD). The best angle values are therefore the ones leading to the lowest THD. The THD is a quantifiable expression for determining how much the signal has been distorted. The greater are the amplitudes of the harmonics, the greater are the distortions. The THD is defined by:

$$THD = \sqrt{\sum_{n=2}^{\infty} \left(\frac{1}{n} \sum_{i=1}^{p=4} \cos n\theta_i\right)^2} / \sum_{i=1}^{p=4} \cos \theta_i .$$
(9)

Choosing the switching angles based on this criteria, the multiple switching angle solutions given in Fig. 5 reduce to the single set of solutions given in Fig. 6, and the corresponding THD is shown in Fig. 7.

The control of an AMI with the HES in a real-time application requires to memorize all the switching angles. A considerable computational memory space must therefore be involved for the implementation of this control law.



Fig. 5. All switching angles versus *r*



Fig. 6. Switching angles versus r leading to the lowest THD

B) Application of ANNs: ANNs have gained increasing popularity and have demonstrated superior results compared to alternative methods in many studies. Indeed, ANNs are able to map underlying relationship between input and output data without prior understanding of the process under investigation. This mapping is achieved by adjusting their internal parameters called weights from data. This process is called the learning or the training process. Their interest comes also from their generalization capabilities, i.e., their ability to deliver estimated responses to inputs that were not seen during training. Hence, the application of ANNs to complex relationships and processes makes them highly attractive for different types of modern problems [8, 12].



Fig. 7. THD versus *r* for the switching angles that result in the lowest total harmonic distortion

We use a neural network to learn the switching angles previously provided by the Newton-Raphson method. The approach aims to replace the painful memorization of the angles in order to make its implementation realizable in a real-time application. MLPs [9] are well suited for this task. Associated to the backpropagation learning rule, they are known as universal approximators [8].

An MLP network is composed of a number of identical units called neurons organized in layers, with those on one layer connected to those on the next layer (except for the last layer or output layer). Indeed, MLPs architecture is structured into an input layer of neurons, one or more hidden layers and one output layer. Neurons belonging to adjacent layers are usually fully connected and the activation function of the neurons is generally sigmoidal or linear. In fact, the various types and architectures are identified both by the different topologies adopted for the connections and by the choice of the activation function.

Some parameters of ANNs can not be determined from an analytical analysis of the process under investigation. This is the case of the number of hidden layers and the number of neurons belonging to them. Consequently, they have to be determined experimentally according to the precision which is desired for the estimation. The number of inputs and outputs depends from the considered process. In our application, the MLP has to map the underlying relationship between the modulation rate (input) and the pswitching angles (output). The MLP is thus composed by one input neuron and p output neurons.

The MLP must be trained in order to adjust and to find the adequate weights. This is achieved by using probabilistic learning techniques and with data from the process under investigation. The training data consists of the inputs R and the corresponding desired output vectors S:

$$R = [r(1) \dots r(l) \dots r(n)], \tag{10}$$

$$S = [S(1) \dots S(l) \dots S(n)] = \begin{bmatrix} \theta_1(1) & \cdots & \theta_1(l) & \cdots & \theta_1(n) \\ \vdots & \vdots & & \vdots \\ \theta_p(1) & \cdots & \theta_p(l) & \cdots & \theta_p(n) \end{bmatrix}.$$
(11)

In the last two expressions, l = 1...n, where *n* is the number of examples. For a given input r(l), the MLP

computes an estimated output vector $\hat{S}(l) = [\hat{\theta}_1(l) \dots \hat{\theta}_p(l)]$ that must be as close as possible to the ideal desired output S(l). The difference $E(l) = (\hat{S}(l) - S(l))^2$ constitutes the squared output error for example *l* that is used by the training algorithm to correct the weights of the neurons. This is repeated for the *n* samples composing the training data set until convergence is reached. The learning is achieved with the backpropagation algorithm [8].

After the training process, the MLP is able to estimate the angles corresponding to an input r(l). In other words, the MLP has learned the functions $\theta_i = f_i(r)$ with i = 1...4. By approximating these functions, the MLP will be able to deliver the angles for the real-time control of the inverter.

Results: learning performance

The MLP is applied for canceling harmonics 5, 7 and 11. The training set is elaborated from the Newton-Raphson method and the optimal angles are the ones resulting in the lowest THD when several solutions exist.

An MLP with 12 neurons in one hidden layer is used with a training set of n = 33 examples. These values have been chosen after different experiments, they represents the best compromise between computational costs and performances. The convergence is reached after 1528 epochs, and leads to angle errors less than 0.001 degrees. The outputs from the MLP are therefore very close to the angles given by the Newton-Raphson method. They are represented by Fig. 8. After learning, the MLP is also able to deliver the angles for inputs which were not present in the training set. Theses generalization capabilities are very interesting in our application, the neural controller is therefore always able to deliver the control signals for the inverter. For example, Fig. 9 shows the results obtained for an input which was not in the training set, r(l) = 0.8 which theoretically corresponds to $\theta_1 = 24.6999^\circ$, $\theta_2 = 45.5307^\circ$, $\theta_3 = 57.0398^{\circ}$ and $\theta_4 = 68.8887^{\circ}$. Fig. 10 shows the frequency content of V_{ab} which can be compared to Fig. 4 obtained with the MCPWM.



Fig. 8. Switching angles versus r learned by the MLP (•) and calculated with Newton-Raphson method (–)



Fig. 9. Output voltage V_{ab} of the 9-level USAMI controlled by the proposed neural HES (with r(l) = 0.8 and p = 4)



Fig. 10. Frequency content of the output voltage V_{ab} with the proposed neural HES (with r(l) = 0.8 and p = 4)

Performance in Supplying an Asynchronous Machine

In order to evaluate the performance and the robustness of the proposed approach, a 9-level USAMI is used to supply an asynchronous machine with a stator resistance R_s = 4.850 Ω , a rotor resistance R_r = 3.805 Ω , a stator inductance L_s = 0.274H, a rotor inductance L_r = 0.274H, a mutual inductance L_m = 0.258H, P = 2 poles pairs, a rotor inertia J = 0. 031kg.m², and a viscous friction coefficient K_f = 0.00136 Nm.s.rad⁻¹.

The neural HES is compared to the MCPWM strategy in controlling the 9-level USAMI. The objective is to use the proposed neural strategy in order to minimize the harmonics absorbed by the asynchronous machine.

The results of the control based on the MCPWM are presented by Fig. 11 and Fig. 12. This first figure shows the stator current and the electromagnetic torque with significant fluctuations. The second figure shows the frequency content of the stator current. Results by using neural approach with the MLP issued for the previous learning process are presented by Fig. 13 and Fig. 14. By comparing Fig. 12 to Fig. 14, it can be deduced that the neural HES efficiently cancels the harmonics of ranks 5, 7 and 11 from the output voltage V_{ab} . Moreover, the amplitudes of the harmonic distortions are very small compared to the amplitude of the fundamental component.



Fig. 11. Stator current (top) and electromagnetic torque (bottom) of the asynchronous machine fed by a 9-level USAMI controlled by the MCPWM

Performances obtained with both methods are summarized in table 1. The THD measured on V_{ab} and resulting from the neural approach of the HES is smaller than the one obtained with the MCPWM method. The

THD measured on the stator current i_{as} is reduced by a factor 2.63 with the neural HES compared to the MCPWM method. The control is thus optimized with the neural HES in order to avoid the asynchronous machine to absorb harmonics.



Fig. 12. Frequency content of the stator current of the asynchronous machine fed by a 9-level USAMI controlled by the MCPWM



Fig. 13. Stator current (top) and electromagnetic torque (bottom) of the asynchronous machine fed by a 9-level USAMI controlled by the proposed neural HE



Fig. 14. Frequency content of the stator current of the asynchronous machine fed by a 9-level USAMI controlled by the proposed neural HES

Table 1. Performances of the control methods

Control method	V _{ab} THD (%)	<i>i_{as}</i> THD (%)	f _{Cem} (Hz)	Δ_{Cem} (Nm)	Nb of θ_i
MCPWM	9.19	5.05	f	1.77	2 <i>m</i> = 48
Neural HES	7.66	1.92	2 <i>f</i>	1.31	4 <i>p</i> = 16

It can also be seen that the electromagnetic torque continuously oscillates at a frequency f with the MCPWM

method (because of the harmonics of rank 2 and 4 which are present in the output voltage). The torque oscillates at 2f with the neural approach. The neural method also reduced the number of switching angles by a factor 3 compared to the MCPWM method which is highly appreciated for the electronic devices.

Conclusions

The control strategy of an inverter used to feed an asynchronous machine is crucial and determines the performances of the motor task. In this study, we propose a low-cost neural implementation of a HES to control a uniform step asymmetrical 9-level inverter. A theoretical analysis of the proposed solving algorithm with neural networks is provided. The neural implementation of the HES uses very few computational costs and is therefore well suited for real-time applications. This neural approach is compared to the MCPWM strategy. Simulation results are given to show the high performance and technical advantages of the neural implementation of the HES for the control of a uniform step asymmetrical 9-level inverter. In the motor supply application, the neural method efficiently cancels the harmonic distortions and ensures a highest quality torque. Moreover, the neural controller allows reducing the switching losses and prolonging the life cycle of the electronic devices.

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A neural implementation of a harmonic elimination strategy for the control a uniform step asymmetrical 9-level inverter is proposed and described in this paper. A Multi-Layer Perceptrons (MLP) neural network is used to approximate the mapping between the modulation rate and the required switching angles. After learning, the neural network generates the appropriate switching angles for the inverter. This leads to a low-computational-cost neural controller which is therefore well suited for real-time applications. This neural approach is compared to the well-known Multi-Carrier Pulse-Width Modulation (MCPWM). Simulation results demonstrate the technical advantages of the neural implementation of the harmonic elimination strategy over the conventional method for the control of an uniform step asymmetrical 9-level inverter. The approach is used to supply an asynchronous machine and results show that the neural method ensures a highest quality torque by efficiently canceling the harmonics generated by the inverter. Ill. 13, bibl. 12, tabl. 1 (in English; abstracts in English, Russian and Lithuanian).

Р. Талеб, А. Мероуфел. Контроль асиметрического многоуровневого преобразователя с применением невроновых сетей // Электроника и электротехника. – Каунас: Технология, 2009. – № 8(96). – С. 93–98.

Предложен и описан асиметрический 9-и уровневый преобразователь, предназначенный для контроля одинаковых шагов в нейроновых сетях, применяя гармоническую систему элиминирования. Для сочетания степени модуляции и углов переключения применяется MLP нейроновая сеть. Обученная нейронная сеть может генерировать соответствующие углы переключения для преобразователя. Это позволяет нейронному управляющему механизму выполнять расчеты в системах, действующих в реальном времени, обеспечивая небольшие затраты. Результаты выполненных исследований могут быть применены в асинхронных машинах, что позволило бы уменьшить преобразователем сгенерированные гармоники. Ил. 13, библ. 12, табл. 1 (на английском языке; рефераты на английском, русском и литовском яз.).

R. Taleb, A. Meroufel. Asimetrinio daugialygio keitiklio kontrolė naudojant neuroninius tinklus // Elektronika ir elektrotechnika. – Kaunas: Technologija, 2009. – Nr. 8(96). – P. 93–98.

Aprašytas ir pasiūlytas asimetrinis devynių lygių keitiklis, skirtas vienodiems žingsniams neuroniniuose tinkluose kontroliuoti taikant harmoninę eliminavimo sistemą. MLP neuroninis tinklas naudojamas derinti moduliacijos laipsniui ir perjungimo kampams. Apmokytas neuroninis tinklas gali generuoti keitikliui atitinkamus perjungimo kampus. Tai leidžia neuroniniam valdikliui atlikti skaičiavimus realiu laiku veikiančiose sistemose esant mažoms išlaidoms. Atliktas neuroninio tinklo tyrimas palygintas su MCPWM moduliacija. Modeliavimo rezultatai parodo techninių galimybių pranašumas. Atliktas tyrimas gali būti taikomas asinchroninėse mašinose, kas leistų užtikrinti maksimalų sukimo momentą efektyviai sumažinant keitiklio sugeneruotas harmonikas. II. 13, bibl. 12, lent. 1 (anglų kalba; santraukos anglų, rusų ir lietuvių k.).