Optimal Design of Lifting Platform Balance Control Algorithm: Co-Simulation and Experiment

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Abstract—The paper deals with balance control problem of lifting platform, collecting detailed first-hand information on its operation in reality. Sums up main challenges to be faced under processing of balance control. Recommends creative and representative control algorithms, comprehensively analysed basing on target platform developed by authors with respective following verification by simulation and testing. Relevant study was performed under three following steps: mathematical modelling, control system design and system verification. Therefore, dynamic model and ADAMS model have been established first based on actual structure of lifting platform. Next, a suitable control algorithm was selected and parameters of target models were set up using ADAMS/MATLAB co-simulation. Finally, both simulation and test results have been verified and compared to show their coincidence. It was found that control algorithms recommended in this paper can effectively improve as stability, reliability as well as security of operation of the lifting platform and can solve as a result the balance control problem of lifting platform at some extent in practice.

Index Terms—ADAMS; balance control; co-simulation; lifting platform; MATLAB.

I. INTRODUCTION

In recent years, lifting platforms have been extensively used for military, industry and civilian purposes. Therefore, the study on its balance control is paid more and more attention. For example, J. Chao sets up an electro-pneumatic stabilized platform driven by pneumatic muscles, and adopts an adaptive robust levelling control strategy based on the coupled MIMO system dynamics to remain balance of platform [1]. In turn, J. Zhang establishes dynamic model of vehicle platform, and recommends a method to achieve excellent dynamic performance of platform levelling process by using repeated balance control strategy [2]. The balance control system for micro platform of non-probe near field optical microscope, which is based on multi-point real-time

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detection and fuzzy adaptive PID control algorithm is discussed by some researchers [3].

This paper presents the developed testing model of the mobile platform installed on a wheeled vehicle. For this purpose, its dynamic model has been derived and respective PID-rule-based control algorithm, which allows direct rotation around X and Z axes to compensate for errors of unbalance angle, has been recommended. Estimation of effectiveness of control algorithm was performed by means of ADAMS and MATLAB Simulink co-simulation. Finally, analysis of simulation and experiment results shows that, satisfactory performance can be achieved when combining the control algorithm with properly selected PID regulator parameters.

II. MODEL CREATION

A. Lifting Platform Design

In order to ensure smooth operation of the lifting platform, it must possess at least three degrees of freedom (DOF) [4]–[6], that is, motion along Y axis, rotation around X and Z axes [7]. The structure of lifting platform indicates that each rotating DOF is achieved by one electrical push rod and four revolute joints, which are fixed in the middle of rotating plane and at both ends of electrical push rod. The actual structure of prototype vehicle with lifting platform, which is used as a simulation and testing model in this paper, is shown in Fig. 1.

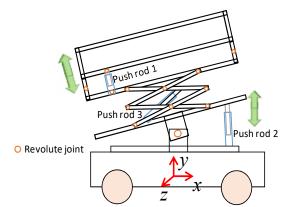


Fig. 1. Structure diagram of lifting platform.

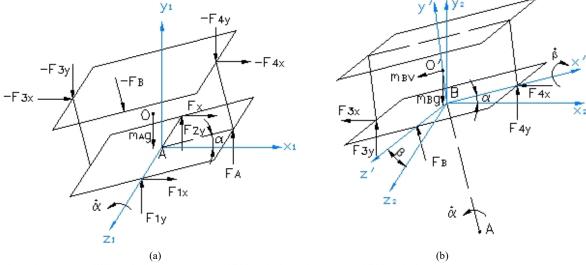


Fig. 2. Schematic structure of lifting platform: (a) - part A of lifting platform; (b) - part B of lifting platform.

B. Dynamic Model

A properly developed mathematical model enables system operation to be examined through experiments, without the need to build a physical system [4]. You can then perform various modifications of the mathematical model taking into account the influence of various input quantities and their values.

In first stage of study, the model of the developed lifting platform with rotation around X and Z axis has been established. To simplify the calculation, it was assumed that two push rods are located on a vertical plane and only subjected to axial direction force. The platform was then divided into two planes A and B with the centres of gravity O and O', which do not change location when lifting or levelling (Fig. 2).

Rectangular coordinate systems $O_{1-X1Y1Z1}$ and $O_{2-X2Y2Z2}$ were positioned in the middle of the Part A's and B's bottom, representing upper and lower part of lifting platform respectively. To simplify the calculation of dynamic model, the coordinate system of lifting platform $O_{2-X^{*}Y^{*}Z^{*}}$ has been referred to part B, wherein, α is obliquity of X axis, β is obliquity of Z axis, and F_A , F_B are supporting forces of each push rod. As a result, the equation of motion of part A can describe by the formula

$$J_{A}\dot{\alpha} = F_{A} \times \frac{L_{1}}{2} \times \cos \alpha + m_{A}g \times \times \frac{h_{1}}{2} \times \tan \alpha - F_{3y} \times \frac{L_{1}}{2} \times \cos \alpha + F_{4y} \times \frac{L_{1}}{2} \times \cos \alpha + F_{3x} \left(h_{1} \times \cos \alpha - \frac{L_{1}}{2} \times \sin \alpha \right) + F_{4x} \left(h_{1} \times \cos \alpha + \frac{L_{1}}{2} \times \sin \alpha \right), \tag{1}$$

where the part A is rotated only around Z1 axis, and $\dot{\alpha}$ is its rotational angular velocity.

Since, resultant force has been transmitted to Z1 axis, therefore, mechanical equilibrium equations are as follows:

$$F_{1x} + F_{2x} - F_{3x} - F_{4x} - F_{8x} \sin \alpha = 0,$$
 (2)

$$(F_{1x} - F_{2x} - F_B \times \sin \alpha) \times \frac{L_2}{2} = 0, \tag{3}$$

$$m_A g - F_A - F_B \times \cos \alpha - F_{1y} - F_{2y} - F_{3y} - F_{4y} = 0,$$
 (4)

$$(F_{2y} - F_{1y} - F_B \times \cos \alpha) \times \frac{L_2}{2} = 0.$$
 (5)

As regards the part B it is allowed to rotate both around the Z and X' axes. Whereas, $\dot{\beta}$ is the rotational angular velocity around X' axis and β is the angle between the bottom and horizontal planes.

The equation of rotational motion around X' axis has the form

$$J_B \times \dot{\beta} = F_B \times \frac{L_2}{2} \times \cos \beta, \tag{6}$$

whereas equation of rotation around Z_1 axis can be expressed as:

$$m_B \ddot{\alpha} \times \left(h + \frac{h_1}{2} \times \cos \alpha \right) =$$

$$= (F_{3x} + F_{4x}) \times \cos \alpha + m_B g \times \sin \alpha, \tag{7}$$

$$m_B \dot{\alpha}^2 h = m_B g \cos \alpha - (F_{3Y} - F_{4Y}) \sin \alpha - F_B \cos \alpha, \quad (8)$$

where J_A is rotational inertia of part A around Z axis, J_B is rotational inertia of part B around X' axis, mA and mB are mass of part A and B, L_1 and L_2 are length and width of platform respectively, h_1 is height of part A, h_2 is height of part B, and h is distance between Z_1 and Z_2 axes.

III. CONTROL STRATEGY

Currently two control algorithms are used for balance control strategy: displacement error control algorithm (DEC) and angle error control algorithm (AEC) [8]–[10]. The DEC is used to make system adjustment, that is, fixes one point, and

then detects and eliminates a position error between the fixed point and removal points. On the contrary, AEC is used to detect angle error and decrease it to 0 degree by controlling systematic movement. Taking into account the convenience of detection, authors applied the AEC algorithm. Flow chart of balance control of AEC [11] is shown in Fig. 3.

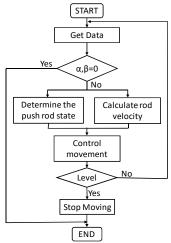


Fig. 3. Flow chart of balance control.

At first, angle information (α, β) is obtained from sensor and compared with ideal angle (0°) . If $\alpha > 0^\circ$, rod 1 needs to drop down to decrease angle. If $\alpha < 0^\circ$, rod 1 needs to rise up to increase angle. When $\alpha = 0^\circ$, rod 1 will not adjust. Because the ideal angel $(\alpha = 0^\circ)$ is not sustained in practice, it was necessary to set up an adjustable range to improve stability of the balance control.

IV. SIMULATION METHOD

A. ADAMS Model

Under bump, slope and hollow road conditions, the obliquity and stability of the lifting platform are greatly affected by nonlinear characteristics of push-rods, lifting system. Therefore, model that can simply and precisely reproduce dynamic characteristics of these systems is needed. A. Sapietova indicates that ADAMS software is very effective and useful providing right mapping of independent driving characteristics of both push-rods [12].

Considering the analysis of the impact of actual parameters, the respective lifting platform model has been developed using ADAMS program. The simplified procedure can be described as follows:

- 1. Measure dimensions of components.
- 2. Analyse structure of models and determine each movement pair.
- 3. Clarify idea of modelling.
- 4. Conduct modelling and test.

Using ADAMS modelling, the longitudinal velocity, lateral velocity, roll angle, pitch angle, longitudinal displacement and lateral displacement must be calculated. Dynamic characteristics of sub-components, such as push-rods, lifting system, and front and revolution system, can be accurately described by means of a multi-body dynamic analysis. As a result, the developed model, shown in Fig. 4, provides reliable dynamic performance of the platform. As one can see, each component is modelled as a rigid body connected by means of

joint and/or bush to simulate platform's dynamic motion. The basic parameters used for calculation are shown in Table. I.

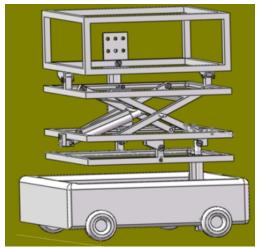


Fig. 4. ADAMS model of orchard vehicle model.

TABLE. I. BASIC PARAMETERS OF ORCHARD VEHICLE.

Item	Value	Item	Value
Width of platform	38 cm	Length of platform	38 cm
Height of part A	25 cm	Height of part B	13 cm
Mass of platform	2 kg	Height of lifting part	20 cm
Maximum thrust of a push rod	50 N	Stroke of a push rod	100 mm
Maximum velocity of a push rod	60 mm/s	Mass of a push rod	0.5 kg

Co-simulation procedure can be deduced from Fig. 5. Under ADAMS/MATLAB co-simulation, longitudinal and lateral forces due to push-rods are calculated first using MATLAB Simulink model and next implemented into ADAMS model. Whereas, longitudinal velocity, lateral velocity, roll angle, pitch angle, longitudinal displacement and lateral displacement parameters are implemented inversely from ADAMS to MATLAB Simulink model [13]–[15].

B. MATLAB/Simulink Model

The interface using S-function API (application programming interface) in ADAMS interacts with Simulink in MATLAB [16]–[18]. We select FORTRAN to create S-function and to import an adam-file, which is open in MATLAB (Fig. 6).

In accordance with the adopted control strategy (Fig. 3) and PID controller, the control system model in MATLAB /Simulink [19] has been set-up as shown in Fig. 5. The process of levelling can be divided into two independent movements along X and Z axes respectively. The Input variable of this model becomes velocity (V_X, V_Y) of two push rods, corresponding to output of PID controller, as well as the angle (α, β) of the lifting platform. Since in practice, the angle variables are affected by vibrations and hardware error, an appropriate white noise was added to angle variable to make simulation results much closer to real situation.

After analysis and research test, it was found that integral coefficient Ki has little influence on levelling process. Therefore, Ki was fixed to be zero and only PD controller was used under further testing.

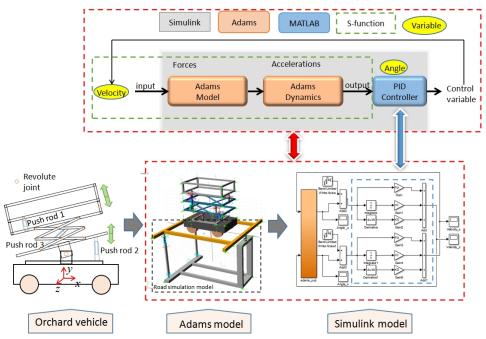


Fig. 5. Co-simulation structure of ADAMS and MATLAB Simulink.

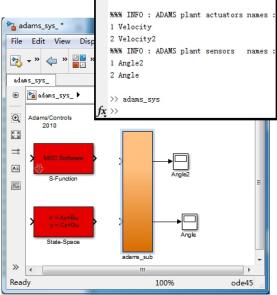


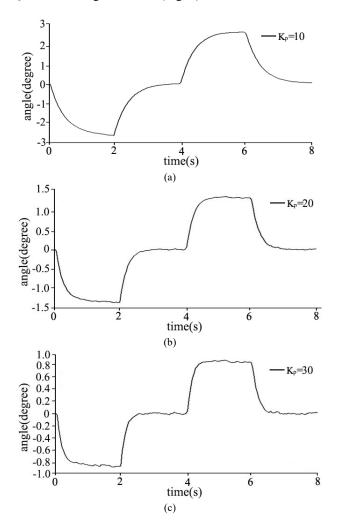
Fig. 6. Adams-file and adams sys of Adams model in MATLAB.

C. Simulation Result and Analysis

It is obvious that the lifting platform motion is impacted by the road conditions. Under our consideration, the sinusoidal road was assumed to be testing road. Therefore, it was necessary to conduct respective preliminary studies to compare specific of motion of vehicle model under different road conditions. It was very helpful to set appropriate road parameters to conduct right co-simulation with ADAMS and MATLAB.

Specifically speaking, the testing vehicle model developed by means of ADAMS was used to conduct motion simulation, which was aimed to find out vehicle motion state under different road conditions. Meanwhile, the vehicle parameters (including velocity, pitching angle, pitching angular velocity, and so on) were measured and analysed using ADAMS/PostProssecor module. The longitudinal amplitude was 0.2 m and horizontal length was 1 m of each sinusoid simulation road. Its task was to examine the correct operation

of control system and proper selection of values of K_p and K_d coefficients, (simulation was regarded as PID parameters tuning process) [20]. At first, the response of the control system to K_p variation was checked. The oscillation was found to be inevitable. However, the most convenient value of K_p is in the range of 20–30 (Fig. 7).



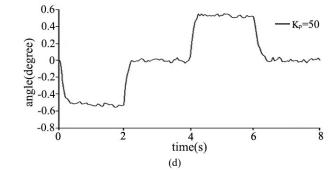


Fig. 7. Co-simulation results of K_p optimization: (a) $-K_p = 10$, $K_d = 0$; (b) $-K_p = 20$, $K_d = 0$; (c) $-K_p = 30$, $K_d = 0$; (d) $-K_p = 50$, $K_d = 0$.

The investigations have indicated a great influence of the K_P value on accuracy, adjustment time and oscillation level of the control system. Specifically speaking, the regulation accuracy and oscillation of platform increases as well as an adjustment time with the increase of K_P (Fig. 7). Therefore, in order to ensure proper operation of the system, the value of K_P should be limited to some extent.

According to the analysis results it can be concluded that proper selection of K_p can improve stability and rapidity of control system. And K_d value affects dynamic characteristics (Fig. 8).

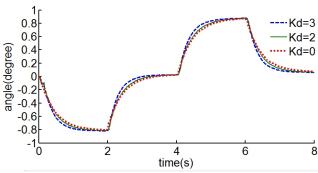


Fig. 8. Co-simulation results of K_d optimization ($K_p = 10$).

For example, when value of Kd is equal to zero and Kp is very small ($K_p = 10$), the response is slow. But with the increase of Kd, which from 0 to 3, the rapidity of control system improved obviously. The performance at the initial stage is accelerated, whereas, the resultant adjustment time increases. It can be imagined that with the adjustment of Kp simultaneously, the stability will increase finally. Therefore, all above mentioned cases have to be taken into account under selection of the value Kd and Kp

V. EXPERIMENT RESULTS

It is obvious that control of a full-sized vehicle under different conditions of operation is difficult to conduct in practice (unstable driven application which involves vehicle rollover and tip-over). Therefore, the testing vehicle model was established to test control algorithm, which was mentioned (Fig. 9). The developed control algorithm was able to be validated with the scaled vehicle since the lateral and vertical dynamics of testing model are similar to those of a full-sized device.

For real-time data acquisition and control, a microcontroller (STM32F103ZET6) of STM

microelectronics was employed. The MPU6050 from STM which combines a 3-axis gyroscope, 3-axis accelerometer and a digital motion processor TM(DMP) were used to measure acceleration and angle rate respectively [21]–[24]. It is placed near to the C.G. of the vehicle to measure the yaw, roll, pitch angles and their rates (Fig. 10).

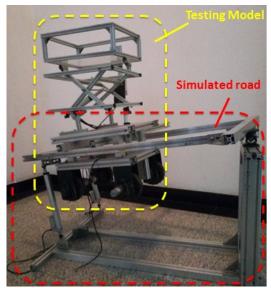


Fig. 9. Testing model and simulated road.

The push rod was driven by DC geared motor (SK3530). The microcontroller samples data from sensors and wirelessly sends them to a ZigBee receiver connected to a computer. The testing results of angle, angle velocity, acceleration and push rod speed are stored in the computer and displayed by real-time testing software, which was developed in C++ language.

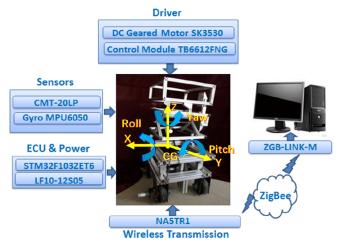


Fig. 10. Main structure of experimental system.



Fig. 11. Main control and driving modules.

The main page of the testing software and its parameter setting can be seen from Fig. 12.

Under the test, the influence of K_P and K_d value on performance of the control system was checked. It was found that simulation and test results indicate high consistency (compare Fig. 13 and Fig. 14).

For example, when K_p value increases, within a certain range, the rapidity, accuracy, as well as stability of the control system are improved simultaneously. (For too small value of K_p , the lifting platform becomes sluggish). On the contrary, when value of K_p is too high, the lifting platform movement

becomes unstable. It is worth to underline that as the value of K_d increases, the control system accelerates, however, resultant adjustment time increases.

As a result it can be concluded that the PD algorithm adopted in the control system can effectively improve the leveling process, however, with different response to adjustment of K_P and K_d parameters. From Fig. 13, with the increase of K_P , the stability of control effect improves obviously, especially from 60 to 80, the adjustment time is not more than 0.5 s and obliquity α of X axis is not more than 2.2°.

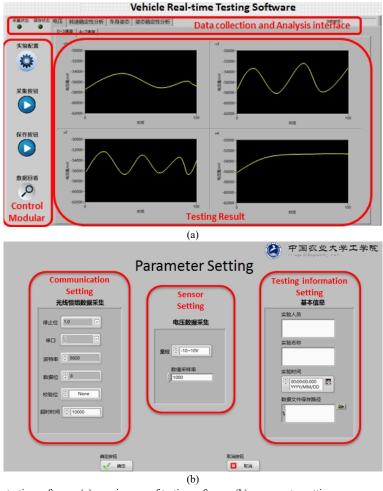


Fig. 12. Orchard vehicle real-time testing software: (a) – main page of testing software; (b) – parameter setting page.

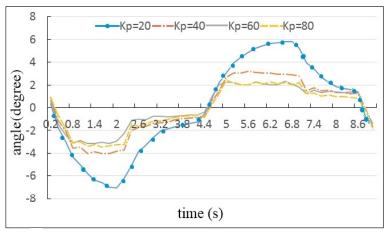


Fig. 13. Test results of K_p vs. obliquity α of X axis ($K_d = 20$).

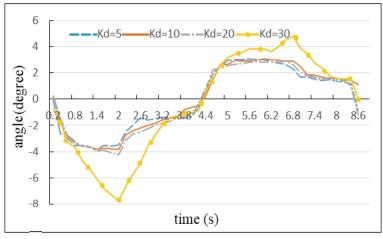


Fig. 14. Test results of K_d vs. obliquity α of X axis ($K_p = 40$).

For the adjustment function of Kd parameter, which is shown in Fig. 14, it can be seen that, from 5 to 20, the control effects is increasing but not notable. That is mainly because of the $K_p=40$, which make a strong control effect of the system, with the increase of Kd can enhance the rapidity of control system directly. But if the Kd is too big (over 20), the control stability will be destroyed also. When $K_d=30$, the fluctuate character of balance system is too big, which cannot obtain the ideal control result.

VI. DISCUSSION

Authors proposed a lifting platform balance control method with PD regulator control algorithm. According to attitude information of platform detected by sensors, such as angles and angular velocities, control algorithm will determine the push rods directions and calculate their velocities. The push rods then generate direct rotation around X and Z axes, which reduces angles of platform. The process is carried out cyclically until the platform achieves a balance.

Through analysis and comparison of co-simulation and vehicle model test, we can draw some interesting, particularly with practical point of view, conclusions. When K_P value increases, the rapidity, accuracy, and stability of the control system can be improved significantly. But when it is over a certain value (it is 50 in simulation), the lifting platform becomes sluggish or unstable. As for Kd, with its increase, response of system accelerates, whereas the total adjustment time increases. Besides, satisfactory performance can be achieved when combine the control algorithm with properly selected PD regulator parameters.

VII. CONCLUSIONS

- 1. Stability of control of the lifting platform has been verified basing on its original structure, designed by authors.
- 2. The PD regulator control algorithm is proposed to compensate for errors of unbalance angles. Co-simulation and model test are conducted to verify the control algorithm.
- 3. In co-simulation, the angles of platform are controlled to small values by adjustment of PD parameters. Obviously, the algorithm can realize balance control of platform. The

scale model test is carried out to verify the control method in a more practical condition. The balance control can also be achieved though it is not as good as that in simulation.

As a result, the stability control algorithm developed and recommended in this paper offers an additional improvement for lifting platform production and can be also helpful under solving related aspects.

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