

# A Novel Supply System for Two-Phase Induction Motor by Single Leg Matrix Converter

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**Abstract**—The paper deals with the novel supply system for two phase induction motor. The system comprises just single leg of matrix converter, and features by reduced number of active and passive components of the supply unit. In comparison to VSI one-leg inverters with rather bulky smoothing capacitors, direct matrix converters operate without DC-link circuit. Analysis using computer simulation under both passive *R-L* and motoric load is given in the paper.

**Index Terms**—Bidirectional switch, induction motor, two-phase system, single leg, matrix converter, power semiconductor devices.

## I. INTRODUCTION

The matrix converter topology has become well known after substitution of thyristor-devices in cycloconverters by switched-off elements acting in high frequency range, in 70s-80s-years [1]–[3], [16]. Matrix converter replace two energy conversion to only one energy conversion, because within converter is not any energy storage element. Classical electric conversion uses DC link converters with rather bulky smoothing capacitors, since direct matrix converters operate without of DC-link circuit. One of the main advantages of that is unity power factor on its input side. Another advantage is that this converter offers sinusoidal input and output harmonic quantity and bi-directional energy flow [3], [8].

Two phase induction motor can be supplied either from two single phase converters or one three-phase VSI inverter [9]–[10], [14]. Another way is using of two matrix converters in half-bridge connection [5]–[7]. Thanks to absence of any energy storage element, the instantaneous power on input must be the same as the power on output side. Unfortunately reactive power input does not have to equal the reactive power output. In MxC it is possible to control the phase angle between the voltages and current on the input – the output phase angle differs from input phase. Another advantage is that the forms of waveforms at the two sides are independent. So the input could be two-phase AC and output DC, or both could be DC, or both could be AC. To save the number power switching elements is also possible to use one-leg connection of the converter [11]–

[13], [20]. The proposed system, in comparison with the conventional system currently used [11]–[13] reduces of the number power switching elements of the converter.

## II. SINGLE LEG MATRIX CONVERTER DESCRIPTION

A single phase matrix converter in basic bridge connection is created by four bidirectional switches (BiS), which allow power flow through the converter from both sides. The basic scheme of half-bridge single-phase matrix converter created by two bi-switches and AC voltage divider is shown in Fig. 1(a), Fig. 1(b).

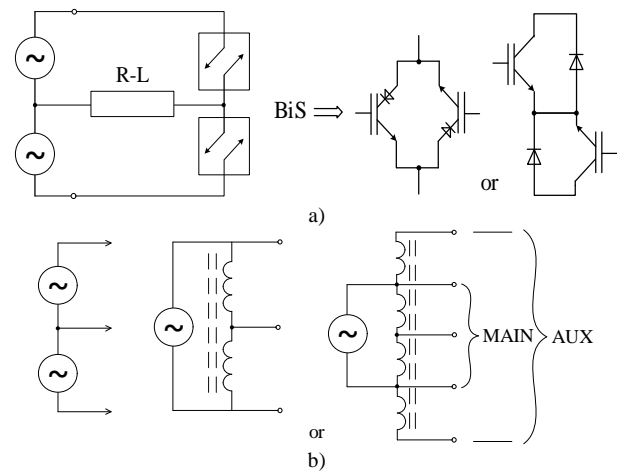


Fig. 1. Basic scheme of half bridge MxC converter (a) with bidirectional switch; inductive divider or autotransformer (b).

The matrix converter requires special semiconductor switches. The matrix converter requires a bidirectional switch, capable of blocking voltage and conducting current in both directions |the energy flow can get from source to load and back. These bidirectional switches, consisting of a pair of devices with turn-off capability, can be reverse blocking RB\_IGBTs or more usually IGBTs with anti-parallel diodes, connected in either a common collector or a common emitter back-to-back arrangement [2]–[3], [5].

The relation between output and input voltages of matrix converter is as follows [3], [7], [8]

$$[v_o(t)] = [M(t)][v_i(t)], \quad (1)$$

where  $v_i(t)$  and  $v_o(t)$  are input- and output voltages,

respectively;  $M(t)$  is modulation matrix

$$[M(t)] = \begin{bmatrix} m_{aA}(t) & m_{aB}(t) \\ m_{bA}(t) & m_{bB}(t) \end{bmatrix}, \quad (2)$$

where  $m_{aA}(t)$ ,  $m_{aB}(t)$ ,  $m_{bA}(t)$ ,  $m_{bB}(t)$  are modulation indexes (time of switched state  $t_{xx}/T_{seq}$ ) with respect to prevent short circuit.

Reciprocally it is valid:

$$[v_i(t)] = [M(t)]^T [v_o(t)], \quad (3)$$

$$[i_i(t)] = [M(t)]^T [i_o(t)], \quad (4)$$

where  $[M(t)]^T$  is transposed matrix.

Principal schematics of single-leg matrix converter (SL\_MxC) supplying two phase induction motor are depicted in Fig. 2 and Fig. 3.

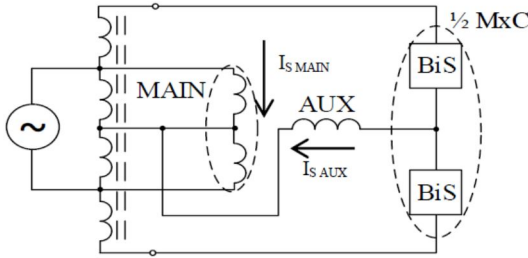


Fig. 2. Schematics of SL\_MxC in full speed operation (50 Hz).

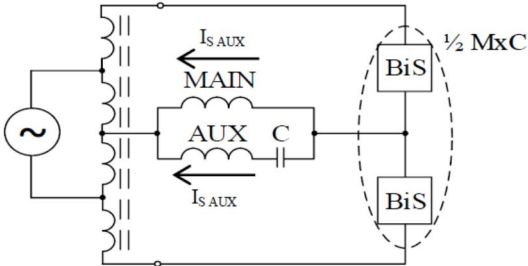


Fig. 3. Schematics of SL\_MxC in reduced speed operation (10 Hz–49 Hz).

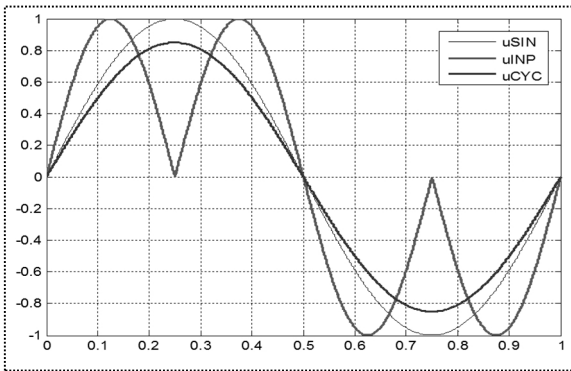


Fig. 4. Two-pulse direct converter fundamental harmonic reaching 0.85% of the main voltage (x: time [n\*T]; y: g-input voltage; b-reference; r-fundamental harmonic).

In full speed regime of operation the main phase of IM is supplied by one half of the main voltage directly; therefore motor should be designed for that voltage. The auxiliary phase is supplied by one-leg matrix converter creating voltage with phase shift by 90 degrees against voltage of the

main phase. Using sinusoidal PWM modulation is possible to obtain fundamental harmonic with maximal value lesser than main voltage fundamental [5], [16]. Principle of obtaining of fundamental harmonic is shown in Fig. 4.

Example of calculation fundamental harmonic for half speed (25 Hz) using Fourier analysis with following integration [4]

$$\begin{aligned} U_{2max(1.HARM)} &= \frac{8}{T} \int_0^{T/4} \cos(2\check{S}t) \cdot \cos(\check{S}t) dt = \\ &= \frac{8}{T} \int_0^{T/4} \frac{1}{2} [\cos(\check{S}t) - \cos(3\check{S}t)] dt = \\ &= \frac{4}{T} \left\{ \frac{1}{\check{S}} [\sin(\check{S}t)]_0^{\frac{T}{4}} - \frac{1}{3\check{S}} [\sin(3\check{S}t)]_0^{\frac{T}{4}} \right\} = \\ &= \frac{4}{T\check{S}} \left\{ \left[ \sin\left(\check{S} \frac{T}{4}\right) - \sin(0) \right] - \frac{1}{3} \left[ \sin\left(3\check{S} \frac{T}{4}\right) - \sin(0) \right] \right\} = \\ &= \frac{2}{f} \left[ (1-0) - \frac{1}{3}(-1-0) \right] = \frac{2}{f} \left( 1 + \frac{1}{3} \right) = \frac{2}{f} \left( 1 + \frac{1}{3} \right) = \\ &= \frac{2}{f} \times \frac{4}{3} \approx 0.85 \Rightarrow 85\%. \end{aligned} \quad (5)$$

This value is varied in full range of the speed from 0.85 to 0.82. Thus, the RMS value of the output voltage of the one-leg converter should be (1.15÷1.18) times greater than requested voltage of the main phase of the system.

In the reduced speed regime of operation both the main- and auxiliary phases of IM are supplied by one-leg of matrix converter; the main one directly; the auxiliary through the capacitor which provides phase shift 90 degrees.

### III. SINGLE LEG MATRIX CONVERTER OPERATION

Single Leg Matrix Converter is dedicated for supplying of two phase induction motor. Model of such a motor is known [13]–[15], [17]–[19]. So, the electric machine being considered may be described by the following set of ordinary differential equations in the stator reference coordinate frame under the commonly used simplifying assumptions:

$$u_{sr} = R_{sr} i_{sr} + L_{sr} \frac{di_{sr}}{dt} + L_{Mr} \frac{di_{rr}}{dt}, \quad (6)$$

$$u_{ss} = R_{ss} i_{ss} + L_{ss} \frac{di_{ss}}{dt} + L_{Ms} \frac{di_{rs}}{dt}, \quad (7)$$

$$\begin{aligned} 0 &= R_{rr} i_{rr} + L_{sr} \frac{di_{rr}}{dt} + L_{Mr} \frac{di_{sr}}{dt} + \\ &+ \frac{1}{N} \check{S}_m (L_{rs} i_{rs} + L_{Ms} i_{ss}), \end{aligned} \quad (8)$$

$$\begin{aligned} 0 &= R_{rs} i_{rs} + L_{rs} \frac{di_{rs}}{dt} + L_{Ms} \frac{di_{ss}}{dt} - \\ &- N \check{S}_m (L_{rr} i_{rr} + L_{Mr} i_{sr}), \end{aligned} \quad (9)$$

$$\begin{aligned} T_e &= pp \left[ N (L_{rr} i_{rr} + L_{Mr} i_{sr}) i_{rs} - \right. \\ &\left. - \frac{1}{N} (L_{rs} i_{rs} + L_{Ms} i_{ss}) i_{rr} \right], \end{aligned} \quad (10)$$

$$T_e = T_{load} + J \frac{d\tilde{S}_m}{dt}, \quad (11)$$

where  $N$  is the ratio between the effective numbers of turns in the auxiliary and the main stator windings;  $\tilde{S}_m$  – mechanical angular speed, and  $pp$  – is the number of pole pairs. Stator voltages  $u_{sR}$  and  $u_{sS}$  of main and auxiliary windings are presented in Fig. 5 in full speed, and reduced speed operation.

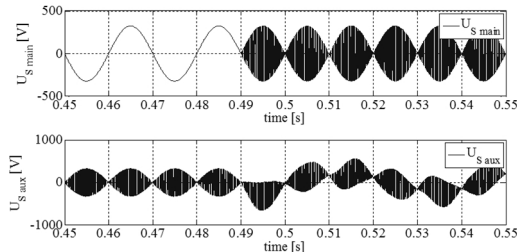


Fig. 5. Creating main and auxiliary voltages of SL\_MxC in full speed 50 Hz (a), and reduced speed 25 Hz operation (b).

Stability of the system is provided by current feed-back with hysteresis controller. Referenced current corresponds to the mechanical load. Speed feed-back loop is not used, so far. As a main problem is to estimate and provide the optimal value of capacitance of the run capacitor to be put in series with the auxiliary winding. Its value can be calculated by one or more methods [13], [18], [21], [22], e.g: using the double revolving field theory, and others. Practical solution leads to switched capacitors. One of the best ways to change the capacitance is to introduce the PWM-controlled choppers between the capacitors. Using these choppers, the capacitors can be switched on and off respectively thus supporting minimal switching losses.

#### IV. SIMULATION OF SL\_MxC UNDER R-L LOAD

The analysis of matrix converter is simulated using the Matlab-Simulink package. All simulations were calculated for source voltage 230 V, 50 Hz, load resistance  $R = 64 \Omega$ , load inductance  $L = 0.001$  H. Current waveforms are shown in Fig. 6 without- and Fig. 7 with capacitor  $C = 8 -F$ .

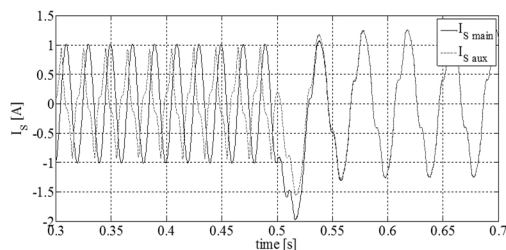


Fig. 6. Stator currents of main and auxiliary phases at 50 Hz and 25 Hz without C in auxiliary phase.

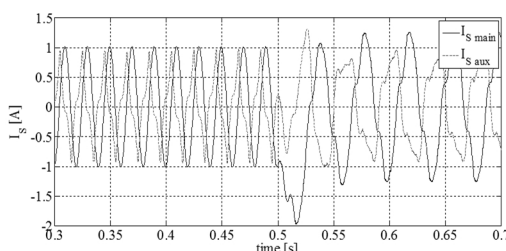


Fig. 7. Stator currents of main and auxiliary phases at 50 Hz and 25 Hz with C in auxiliary phase.

Time waveforms of main and auxiliary phase currents are corresponded to the voltage waveforms at 50 Hz and 25 Hz shown in Fig. 5(a) and Fig. 5(b).

#### V. SIMULATION OF SL\_MxC LOADED BY IM MOTOR

##### A. Parameters of the Simulations

All simulations were calculated using the Matlab-Simulink package for source voltage 230 V, 50 Hz, at calculation step of 10  $\mu$ sec.

Parameters of the two phase motor:

Stator voltage 115 V

Stator resistance  $R_{sR} = 58.85 \Omega$ ;  $R_{sS} = 66.1 \Omega$ ;

$R_r = 80 \Omega$ ;

Stator inductance  $L_{sd} = 1.835$  H;  $L_{sq} = 1.64$  H;

Mutual inductance between rotor and stator  $M_{srd} = 1.74$  H;  $M_{srq} = 1.52$  H;

Moment of inertia  $J = 0.0000488$  kg.m<sup>2</sup>;

Number of pole pairs  $pp = 1$ ;

Capacitance of the capacitor in auxiliary phase  $C = 8 -F$ .

##### B. Simulation Results at Full and Reduced Speed of the Motor

The motor is started-up onto nominal speed. At time instant of 0.5 sec is done step change of frequency from 50 Hz to 25 Hz. At time instant of 1 sec is done step change of the load from 0 N.m to 0.1 N.m.

Stator current waveforms of main and auxiliary phases at 50 Hz and 25 Hz are depicted in Fig. 8.

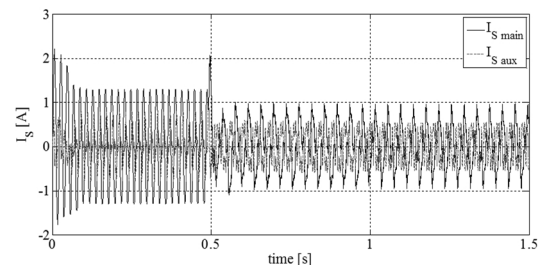


Fig. 8. Stator currents of main and auxiliary winding in full speed (a) and reduced speed regime.

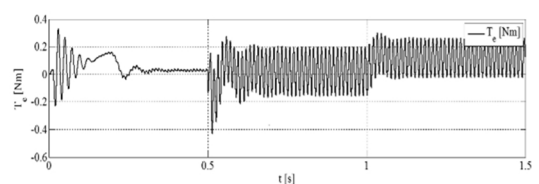


Fig. 9. Electromagnetic torque of the motor in full speed and reduced speed regimes.

Time waveforms of main and auxiliary phases in full- and reduced speed regimes of operation are corresponded to the voltage waveforms at 50 Hz and 25 Hz shown in Fig. 5(a) and Fig. 5(b).

Electromagnetic torque of the motor in full speed (50 Hz) and at reduced speed (40 Hz) regimes is shown in Fig. 9.

The torque of the capacitor-run two-phase IM depends on the currents in both the main and the auxiliary windings. Along with the frequency decrease, an impedance of the auxiliary winding grows because of the series-connected capacitor, which reactance is inversely proportional to the

frequency. At the same time, an impedance of the main winding decreases at low frequencies. An effect of electromagnetic torque lowering along with the frequency drop can be explained using the torque equilibrium (8), [22].

Angular speed of the motor in full speed 50 Hz and reduced speed 25 Hz regimes is presented in Fig. 10.

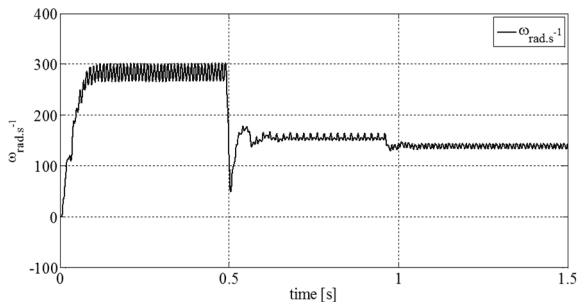


Fig. 10. Angular speed of the motor in full speed and reduced speed regimes.

### C. Discussion to Simulation Results under R-L and Motoric Loads

Above worked-out results under R-L and motoric loads are just preliminary ones because of value of capacitance of the capacitor in auxiliary phase is not optimized, and also that the speed loop has not been used so far. To provide the same value of phase current and consequently torque in both main and auxiliary phases is necessary to boost the voltage of auxiliary phase.

## VI. CONCLUSIONS

The novel supply system for two phase induction motor has been introduced. The system comprises just single leg of matrix converter, and features by reduced number of active and passive components of the converter. The simulation results agree with the theoretical expectations, that the single leg of matrix converter is able to create sinusoidal current waveforms on output side, which is necessary for good working condition of drive systems. One problem is still open – variable capacitance of capacitor in auxiliary phase of the motor. Practical solution leads to switched capacitors; for small power single phase drive is possible operation with fixed run capacitor. From the economic point of it would be nice to use monolithic bidirectional switches which development has been announced based on Mosfet structures. Future work is oriented to investigation of the system in closed speed loop operation, decreasing of torque ripple, optimizing of capacitor value, and efficiency investigation.

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