

## Simulation of Stress Distribution in the Silicon Substrate

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### Introduction

Si oxidation technological process is common using in the semiconductors production process. The oxide, which is growing in thermal oxidation, causes intrinsic stresses in all structure.

In stress, area might be arising dislocations. If it use integrated elements isolation methods such as LOCOS and oxidized trench, thin film deposition in different temperature it'll appear various intrinsic stresses, which increases defects.

By using mathematical simulation program ATHENA was performed mathematical simulation of Si thermal oxidation and thin films deposition technological processes, and was evaluated the distribution of stresses in all semiconductor structure.

### Stress calculation model in the growing oxide

The fabrication of integrated circuit microelectronic structures and devices vitally depends on the thermal oxidation process for the formation of gate dielectrics, device isolation regions, spacer regions, and the ion implantation masks regions. Particularly, the precise controls of silicon dioxide thickness as device geometries continue to scale to nano-dimensions [1].

The Viscous Model calculates stresses in the growing oxide and creates almost the same shape for the silicon oxide interface, as does the Compress model. The stresses in the oxide are calculated as follows:

$$o_{xx} + o_{yy} = \frac{2 \cdot VISCO \cdot \exp\left(\frac{-VISCE}{kT}\right)}{1 - 2 \cdot POISSR} \times \left(\frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y}\right); \quad (1)$$

$$o_{xx} - o_{yy} = 2 \cdot VISCO \cdot \exp\left(\frac{-VISCE}{kT}\right) \times \left(\frac{\partial v_x}{\partial x} - \frac{\partial v_y}{\partial y}\right); \quad (2)$$

$$o_{xy} = VISCO \cdot \exp\left(\frac{-VISCE}{kT}\right) \times \left(\frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y}\right); \quad (3)$$

where  $v_x$  and  $v_y$  are the  $x$  and  $y$  components of flow velocity  $v$  respectively.  $VISCO$  and  $VISCE$  are the pre-exponential and activation energy, respectively for viscosity.

The stress-dependent nonlinear model based on Eyring's work allows a description of the real shape of LOCOS profiles with kinks on the interface. Using equations 1, 2 and 3, the non-linear solver first finds a linear solution for flow velocities and stresses and then uses the stresses obtained to calculate the reduction factors for oxidant diffusivity,  $D_{eff}$ , oxide viscosity,  $\mu$ , and the interface reaction rate constant  $k$  as follows:

$$D_{eff}^{(i)} = D_{eff}^{(i-1)} \cdot \exp\left(\frac{V_d (\sigma_{xx} + \sigma_{yy})}{kT}\right); \quad (4)$$

$$\mu^{(i)} = \mu^{(i-1)} \frac{\left(\frac{\tau V_c}{2kT}\right)}{\sinh\left(\frac{\tau V_c}{2kT}\right)}; \quad (5)$$

$$k^{(i)} = k^{(i-1)} \cdot \exp\left(-\frac{\sigma_r V_r + \sigma_t V_t}{kT}\right); \quad (6)$$

where  $i$  is the iteration  $V_d$ ,  $V_c$ ,  $V_r$ , and  $V_t$  are the activation volumes.  $\tau$  is the total shear stress:

$$\tau = \frac{1}{2} \sqrt{(\sigma_{xx} - \sigma_{yy})^2 + 4\sigma_{xy}^2}; \quad (7)$$

$\sigma_r$  is the normal component of the total stress:

$$\sigma_r = \sigma_{xx} n_x^2 + \sigma_{yy} n_y^2 + 2\sigma_{xy} n_x n_y; \quad (8)$$

$\sigma_t$  is the tangential component of the total stress:

$$\sigma_t = \sigma_{xx} n_y^2 + \sigma_{yy} n_x^2 + 2\sigma_{xy} n_x n_y; \quad (9)$$

where  $n_x$  and  $n_y$  are the  $x$  and  $y$  components of the unit vector normal respectively [2].

### Stress calculation models

There are three ways to calculate stresses generated during semiconductor processing:

1. The first way is to calculate the stresses during viscous oxidation or viscous material reflow.
2. The second way is to calculate the stresses due to thin film intrinsic stress of thermal mismatch.
3. The third way is to follow stress history.

In the cases of the second and third methods, performing a finite element analysis of the material structure solving the similar set of equations as in the case of viscous oxidation. The only difference is the thermal expansion and intrinsic terms added to the right-hand side of equation 1:

$$\sigma_{xx} + \sigma_{yy} - \frac{4(1 + POISS.R)}{1 - 2 \cdot POISS.R} VISC.0 \times \exp\left(\frac{-VISC.E}{KT}\right) \int_{T_2}^{T_1} LCTE + INTRIN.SIG_i \quad (10)$$

The linear coefficient of the material thermal expansion  $LCTE$  can be specified as a function of temperature  $T$ . The film intrinsic stress parameter  $INTRIN.SIG$ .  $T_1$  and  $T_2$  are initial and final temperatures.

If the stress history method is specified, then calculates stresses when the simulation structure changes after etching, deposition, epitaxy, and diffusion processes. The temperature specified for current process step is used in the calculation. The final stress from the previous step is used as a initial condition for the subsequent step [2].

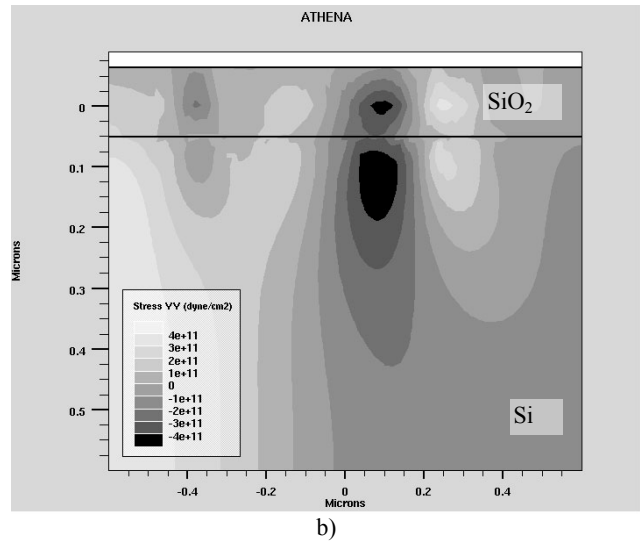
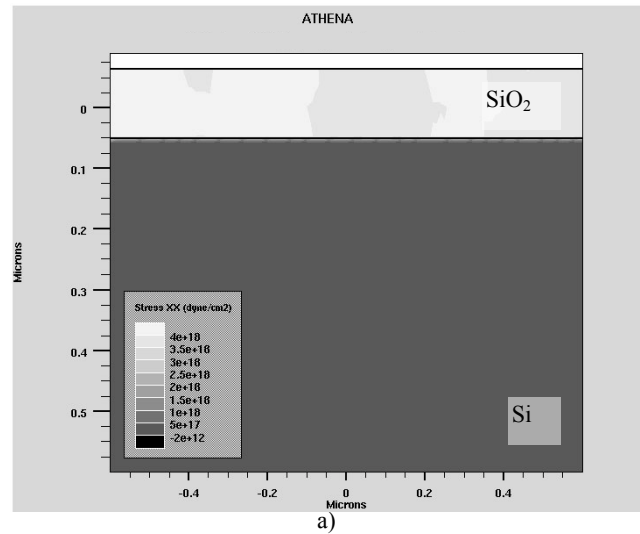
### Simulation of stress distribution

Using mathematical simulation program ATHENA [3] was performed mathematical simulation of planar silicon surface oxidation (Fig. 1, 2, 3). Analyzing stresses in XX plane was observed that biggest stress  $\sim 4 \cdot 10^{18}$  dyne/cm<sup>2</sup> generating in new formed SiO<sub>2</sub> layer. The dyne is a unit of force specified in the centimeter-gram-second. In YY plane lower stress  $\sim 4 \cdot 10^{11}$  dyne/cm<sup>2</sup> distribute in all structure, because the newly formed oxide easy lifts up the previously formed oxide. Since the surface of the oxide is not constrained, the oxide is free to move in this direction so negligible stress is induced normal to the Si-SiO<sub>2</sub> interface.

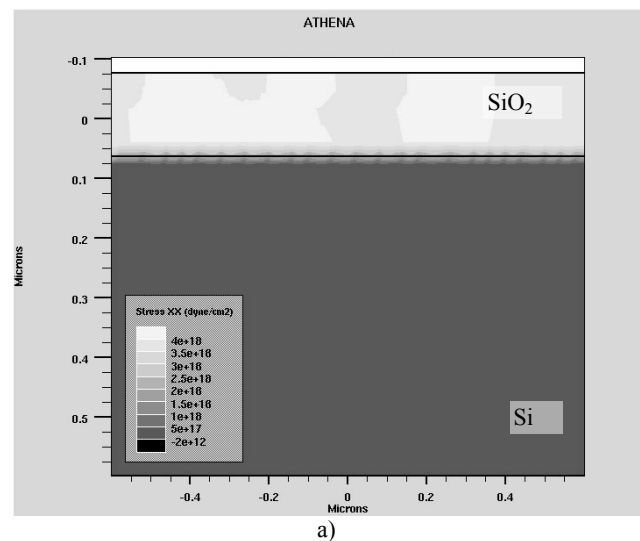
Stress distribution in Si substrate also depends on crystallographic orientation. There were made the oxidation process's mathematical simulation of Si substrates of 100, 110 and 111 crystallographic orientation.

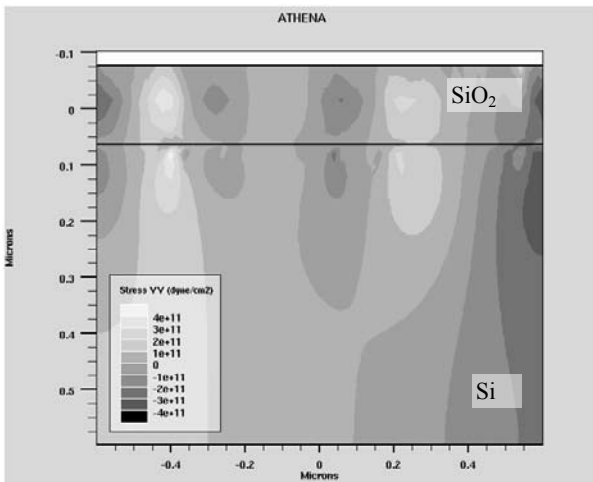
By comparison mathematical simulation results (in figures 1, 2 and 3) was observed when Si substrate

crystallographic orientation is 111 the stresses distribution is more equal.

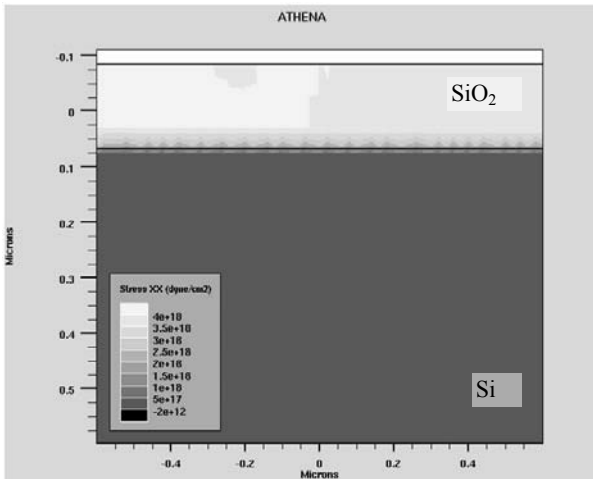


**Fig. 1.** Stress distribution after planar Si wet oxidation: Si crystallographic orientation – 100; oxidation time – 10 min, temperature – 1000 °C; a) – stress distribution in XX plane, b) - stress distribution in YY plane





**Fig. 2.** Stress distribution after planar Si wet oxidation: Si crystallographic orientation – 110; oxidation time – 10 min, temperature – 1000 °C; a) – stress distribution in XX plane, b) - stress distribution in YY plane

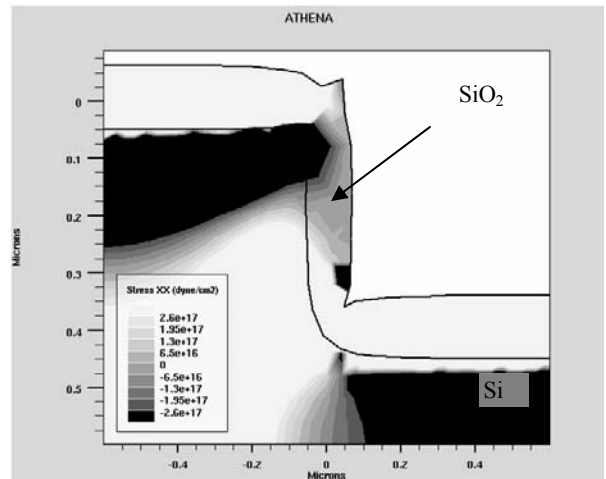


**Fig. 3.** Stress distribution after planar Si wet oxidation: Si crystallographic orientation – 111; oxidation time – 10 min, temperature – 1000 °C; a) – stress distribution in XX plane, b) - stress distribution in YY plane

In non-planar regions such as convex and concave corners of silicon, a strain exerted in the silicon dioxide

and in all structure. Silicon step thermal oxidation is modelled by using mathematical simulation program ATHENA (Fig. 4).

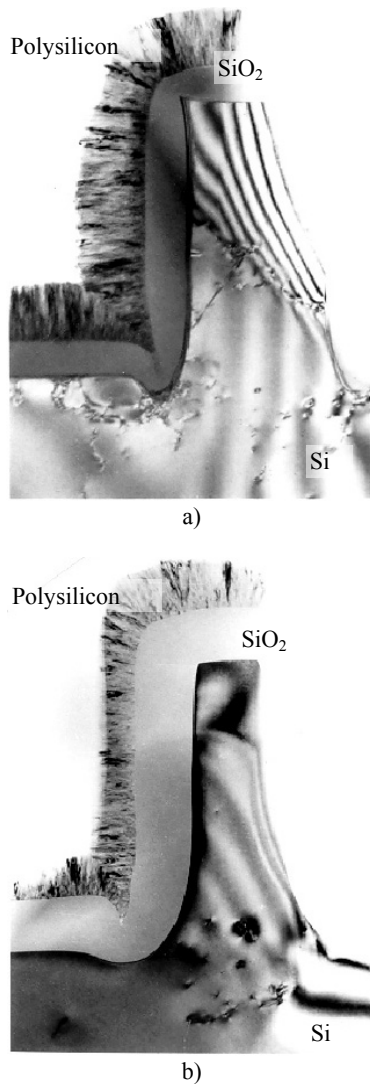
As seen in simulation results the growing oxide starts to crush in the internal corners. In this regions forming stresses  $\sim 2.6 \cdot 10^{17}$  dyne/cm<sup>2</sup> because growing silicon oxide expanding perpendicular to the surface and expanding to the both sides. By analyzing stresses distribution in XX and YY planes the compressing stresses are biggest in the internal corners. This type of stresses appearing in SiO<sub>2</sub> and spreads to Si crystal.



**Fig. 4.** Stress distribution after Si uneven surface wet oxidation: oxidation time – 10 min, temperature – 1000 °C; a) – stress distribution in XX plane, b) - stress distribution in YY plane

As shown in figure 4 stress distributions in XX and YY planes, growing SiO<sub>2</sub> causes stretch effect at Si convex corners, which can arise to  $\sim 2 \cdot 10^{18}$  dyne/cm<sup>2</sup>. Therefore, when oxidizing the silicon of complex surface various character stresses arise in all structure. They can change physical properties of materials and can generate defects or damage all structure (Fig. 5).

The experimental results of silicon oxidation represented in figure 5 [4]. The dark areas show the stress and dislocations in the silicon structure. As we see the defects depends on SiO<sub>2</sub> thickness and on oxidation process temperature.



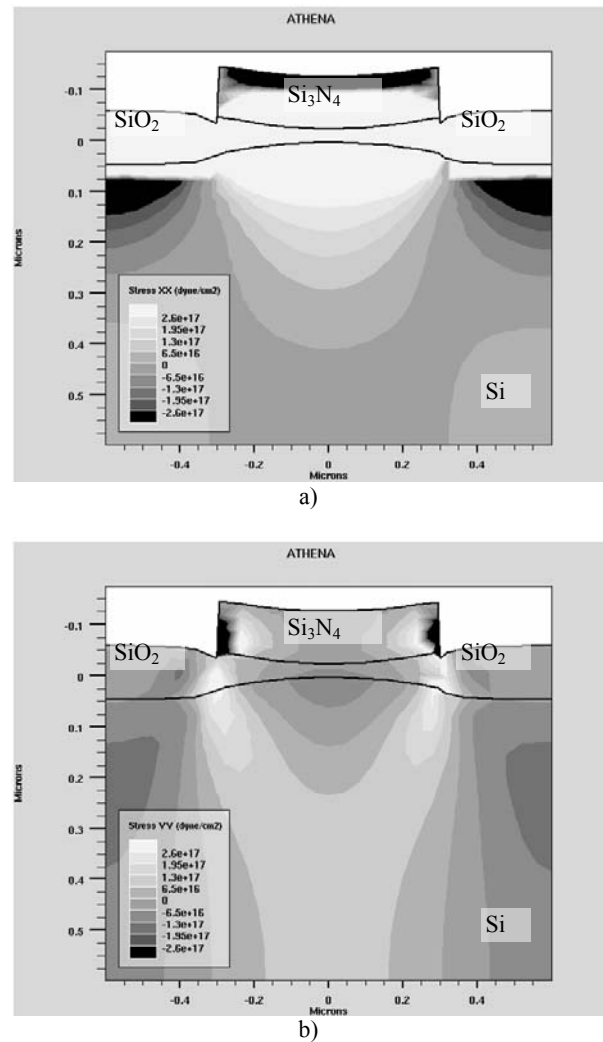
**Fig. 5.** Stress distribution after Si uneven surface wet oxidation: oxidation time – 10 min; a) – oxidation temperature – 950 °C, b) – oxidation temperature – 1100 °C [3]

Local oxidation of silicon (LOCOS) is generally using in microelectronics. LOCOS oxide is using to isolate one integrated elements from another [1, 5, 6]. In this technology thermal silicon oxidation is using also. The main problem is that growing oxide move under  $\text{Si}_3\text{N}_4$  film that rising from the substrate due to generated stress. In this case, the exposed surface became uneven and the defects can occur in protective  $\text{Si}_3\text{N}_4$  film. Mathematical simulation of LOCOS oxidation performed using mathematical simulation program ATHENA. Stresses distributions in XX and YY planes analyzed in accordance with mathematical simulation results (Fig. 6).

The mathematical simulation results demonstrate that the stresses in XX and YY planes distribute in all structure irregular. The stress in growing silicon oxide extends to nearest areas and to thin films. In this case, stress distribution depends on  $\text{Si}_3\text{N}_4$  film elasticity. Figure 6 demonstrate that stress is expanding in all structure by growing LOCOS oxide.

The biggest compression ( $\sim 2.6 \cdot 10^{17}$  dyne/cm<sup>2</sup>) occurs then  $\text{SiO}_2$  lean against  $\text{Si}_3\text{N}_4$  film edges (Fig. 6). It can point up that the biggest stresses occur in the corners of the

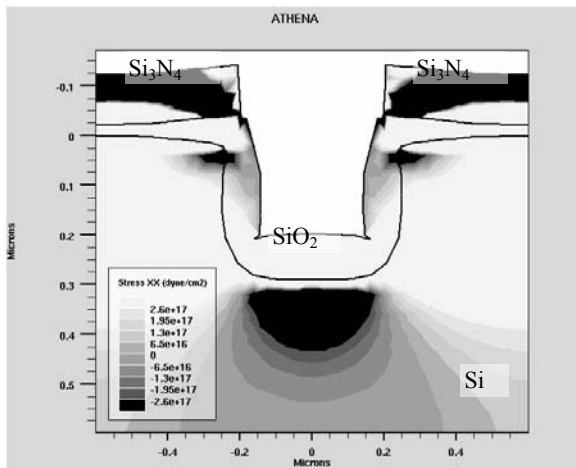
structure. The stresses and grown  $\text{SiO}_2$  form depends on the elasticity of  $\text{Si}_3\text{N}_4$  film. If  $\text{Si}_3\text{N}_4$  film elasticity decreasing, newly forming  $\text{SiO}_2$  must take higher resistant force of  $\text{Si}_3\text{N}_4$  film. Therefore stresses increasing in  $\text{SiO}_2$  layer and in all structure. Dislocations occur then stress reach critical material elasticity.



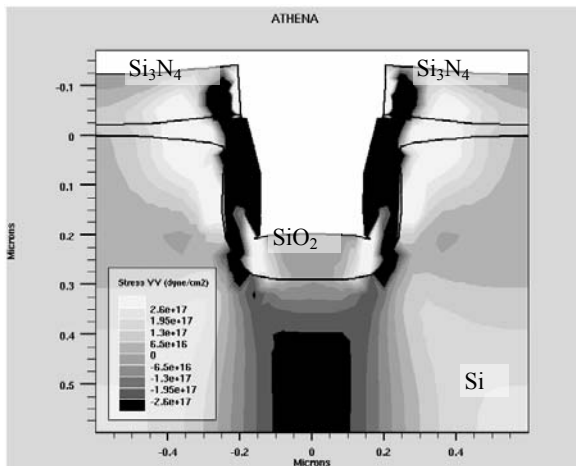
**Fig. 6.** Stress distribution after LOCOS wet oxidation: oxidation time – 10 min, temperature – 1000 °C; a) – stress distribution in XX plane, b) - stress distribution in YY plane

Trenches are popular isolation technologies that also exhibit dislocation generation problems [7]. By using mathematical simulation program ATHENA it was performed simulation of Si trenches oxidation technological operation.

Mathematical simulation results of ion plasma etched trench oxidation represented in figure 7. By analyzing stresses distribution in XX and YY planes was observed that forms wide range of stresses: compression and stretch. Stress distribute deep in all structure. In this case growing silicon oxide move under  $\text{Si}_3\text{N}_4$  film therefore occur additional stress in  $\text{SiO}_2$  and  $\text{Si}_3\text{N}_4$  layers. Very high stress occurs due to trench internal corners then horizontal and vertical growing oxide starting to crush. In first stress appear in silicon oxide layer and distribute to neighbouring regions later. Growing  $\text{SiO}_2$  thickness expanding stress as it shown in figure 7.



a)

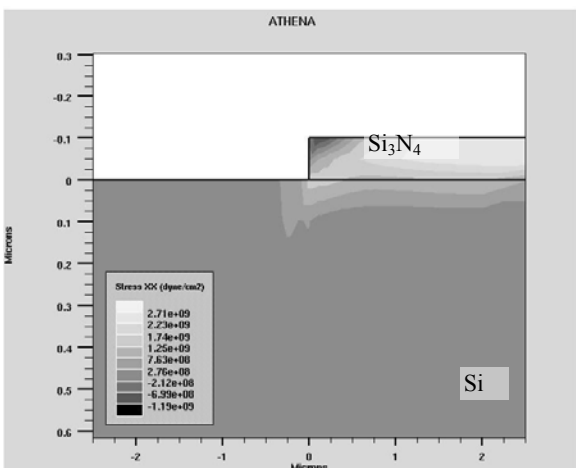


b)

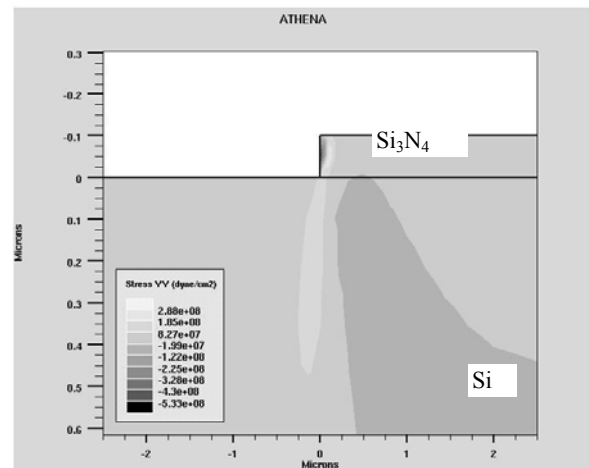
**Fig. 7.** Stress distribution after plasma etched trench wet oxidation: oxidation time – 10 min, temperature – 1000 °C; a) – stress distribution in XX plane, b) - stress distribution in YY plane

Rectangular trench form is forming by plasma-etched technology. This form has a couple internal and external corners. Therefore, very different stresses are generating. The structure can crash due to these stresses. To reduce stresses need to reduce the number of corners.

Mathematical simulation of thin film deposition process results presented at figure 8.



a)



b)

**Fig. 8.** Stress distribution after thin  $\text{Si}_3\text{N}_4$  film deposition: process temperature - 1000 °C; a) – stress distribution in XX plane, b) - stress distribution in YY plane

These simulation results show that the stresses in the Si substrate and thin film arising from nitride layer, which has an intrinsic stress of  $\sim 2.88 \cdot 10^8$  dyne/cm<sup>2</sup> when deposited uniformly. This is thermal mismatch stress in the whole structure as the results of the temperature change.

## Conclusions

1. After oxidation of the silicon of complex surface various character stresses arise in all structure. Observed, that growing oxide causes intrinsic stresses in all structure during thermal oxidation. They can change physical properties of the materials and can generate defects or damage all structure

2. The lower stresses appear in planar regions. The bigger stresses appear in non planar regions. Growing  $\text{SiO}_2$  causes stretch effect at Si convex corners, which can arise to  $\sim -2 \cdot 10^{18}$  dyne/cm<sup>2</sup>. The growing oxide starts to crush in the internal corners. In this regions forming stresses  $\sim 4 \cdot 10^{18}$  dyne/cm<sup>2</sup>. This type of stress appearing in  $\text{SiO}_2$  and spreads to Si crystal.

3. Analyzing stresses distribution after planar silicon surface oxidation in XX plane it was observed that biggest stress  $\sim 4 \cdot 10^{18}$  dyne/cm<sup>2</sup> generating in new formed  $\text{SiO}_2$  layer. In YY plane lower stress  $\sim 4 \cdot 10^{11}$  dyne/cm<sup>2</sup> distribute in all structure.

4. Stress distribution in Si substrate also depends on crystallographic orientation. It was observed when Si substrate crystallographic orientation is 111 the stresses distribution is more equal.

5. After LOCOS oxidation, the stresses distribute in all structure irregular. Stress distribution depends to  $\text{Si}_3\text{N}_4$  film elasticity. The biggest compression ( $\sim 2.6 \cdot 10^{17}$  dyne/cm<sup>2</sup>) occurs then  $\text{SiO}_2$  lean against  $\text{Si}_3\text{N}_4$  film edges. Dislocations occur then stress reach critical material elasticity.

6. Thin film deposition also generates the stresses in all structure. These stress arising due to different thermal expansion coefficient of the silicon substrate and  $\text{Si}_3\text{N}_4$  thin film.

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### **T. Keršys, R. Anilionis, D. Eidukas. Simulation of Stress Distribution in the Silicon Substrate // Electronics and Electrical Engineering. – Kaunas: Technologija, 2007. – No. 4(76). – P. 3–8.**

Si oxidation technological process is common occurrence in the semiconductors production process. The oxide which is growing in thermal oxidation causes intrinsic stresses in all structure. In stress area might be arising dislocations. Various intrinsic stresses appear when using integrated elements isolation methods such as LOCOS and oxidized trench. Thin films such as silicon nitride, silicon oxide and polysilicon are mostly usable in the semiconductors production. These films have the intrinsic stresses, which appear in the films deposition process apropos of different thermal expansion coefficients of the materials. By using mathematical simulation program ATHENA was accomplished mathematical simulation of Si thermal oxidation and thin film deposition technological processes and was evaluated the distribution of stresses in all semiconductor structure, Ill. 8, bibl. 7 (in English; summaries in English, Russian and Lithuanian).

### **T. Кяршис, Р. Анилёнис, Д. Эйдукас. Математическое моделирование распределения натяжений в структуре кремния // Электроника и электротехника. – Каунас: Технология, 2007. – №. 4(76). С. 3–8.**

Для изготовления полупроводниковых приборов чаще всего используется технологический процесс окисления кремния. Во время окислительного процесса возрастающий окисел создает натяжение во всей структуре. В натянутых местах создаётся вероятность появления дислокации. Самые разные натяжения создаются, используя LOCOS и окисление углубления кремния - изоляционные методы интегральных элементов. Для изготовления полупроводниковых приборов также используются тонкие плёнки:  $\text{Si}_3\text{N}_4$ ,  $\text{SiO}_2$ . Эти плёнки имеют внутренние натяжения, которые возникают во время нанесения плёнок. Натяжения возникают из-за разных коэффициентов температурного расширения материалов. Используя программу математического моделирования ATHENA, было произведено моделирование технологических процессов: окисление кремния и нанесение тонких плёнок. Произведён анализ распределения натяжений во всей структуре. Ил. 8, библи. 7 (на английском языке; рефераты на английском, русском и литовском яз.).

### **T. Keršys, R. Anilionis, D. Eidukas. Įtempių pasiskirstymo silicio luste matematinis modeliavimas // Elektronika ir elektrotechnika. – Kaunas: Technologija, 2007. – Nr. 4(76). – P. 3–8.**

Puslaidininkų gamybos procese dažnai taikomas Si oksidavimo technologinis procesas. Terminės oksidacijos metu augantis oksidas sukelia vidinius įtempius visoje struktūroje. Įtempių vietoje atsiranda galimybė susidaryti dislokacijoms. Įvairūs vidiniai įtempiai atsiranda ir taikant integrinių grandynų izoliavimo metodus, tokius kaip LOCOS ir oksiduotas griovelis. Plonos plėvelės, tokios kaip silicio nitridas, silicio oksidas ir polisilicis, dažniausiai yra naudojamos puslaidininkų gamyboje. Šios plėvelės turi vidinius įtempius, kurie atsiranda plėvelių sudarymo metu dėl skirtingų medžiagų temperatūrinių plėtimosi koeficientų. Pasinaudojus matematinio modeliavimo programa ATHENA atliktas Si terminės oksidacijos ir plonų plėvelių sudarymo technologinių procesų matematinis modeliavimas, atsižvelgiant įtempių pasiskirstymą visoje puslaidininkio struktūroje, II. 8, bibl. 7. (anglų kalba; santraukos anglų, rusų ir lietuvių k.).

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