Optimization of VFD Operations for Transporting Equipment of Packages

Lione Urmoniene¹, ², *, Jelena Dikun², ³, Jolanta Januteniene¹
¹Department of Engineering, Klaipeda University, Bijunu St. 17, LT-91225 Klaipeda, Lithuania
²Klaipeda State University of Applied Sciences, Bijunu St. 10, LT-91225 Klaipeda, Lithuania
³Lithuanian Maritime Academy, Kanto St. 7, LT-92123 Klaipeda, Lithuania
lione.urmoniene@ku.lt

Abstract—This study is focused on the efficiency of automated transferring system of packages equipped by variable-frequency drive (VFD) and servo drive motor. It was found that rotation frequency of induction motors and linear speed of servo drive decisively affected the unit efficiency that operates in the periodic mode. The system duty cycle was divided in two separate parts taking into account time spans needed to complete the specific tasks by each separate equipment of the system. In order to reduce the power usage of the system, the duration of each part of cycle was extended. Lowered electricity consumption leads to the extension of each cycle’s stage operating times. Frequencies of motors and linear speed of servo drive motors were optimized depending on cycle stages duration. Optimized frequency and linear speed values were calculated and loaded into motors controllers, and the efficiency of each separate equipment was measured, as well as total efficiency of the system. Experimental system debugging using optimized parameters proved that system efficiency increases up to 60%, and that is closely matched with calculated values.

Index Terms—Energy consumption; Automation; Variable speed drives; Electric motors.

I. INTRODUCTION

Variable frequency drives (VFDs) are widely applied in many common industrial machineries, such as fans, compressors, and pump systems [1]. Many scientific studies and experiments unconditionally confirm the benefits of VFD implementation in the Heating, Ventilation, and Air Conditioning (HVAC) systems. Use of VFD contributes to electrical energy conservation at around 18.3 %–47.1 % and 36.3 %–51.7 % in air conditioning systems in winter and summer time, respectively, and it is more economical than a constant speed converter [2]. Another group of scientists [3] found out that energy savings with VFD reached 45 % in the air conditioning systems. As for the pump, fans, blowers, and compressor drives, the energy savings due to application of VDF can vary from 20 % to 70 % [4], [5].

Nevertheless, there are many new scientific investigations addressed to the efficiency enhancements in the systems controlled by VDF [6], [8] that are comprised of inductive motor and logic controller. Efficiency optimization study [6] suggests focusing attention on the constituent parts of variable frequency drive, especially in lowering the losses in the induction motor. Decrease in rotation speed to 30 % due to VFD in the system of two parallel operating pumps has shown the reduction in consumer power. Reduction up to 66 % of each motor results in energy consumption reduction by 20 % in the system [8]. Power losses elimination in the induction motor [9]–[11], as well as in the drive controlling equipment [7], [11], [13], is of great interest to investigators trying to achieve higher electricity conservation. In work [10], energy efficiency improvement was attained by replacing the inductive motor with permanent magnet motor that results current reducing and allows diminishing annual electricity consumption in installation drive equipment up to 26 %. In study [11], investigators minimized power losses by controlling the flux level in the variable load induction motor up to about 60 % using appropriate drive controlling methods. Nevertheless, described methods involve a complex mathematical computation and have a noise that affects measurement accuracy. Another way, described in [12], to improve VFD efficiency deals with induction motor power factor correction by connecting capacitance in parallel to the motor that leads to the efficiency enchanting in the transmission network Motor-PLC-VFD. Such technique results in the power factor correction from 0.693–0.72 up to 0.96–0.98.

For the higher drive efficiency, different control algorithms (Genetic Algorithm, Particle Swarm Optimization algorithm, Fuzzy Logic and Artificial Neural Network) were used [11]. Although the application of some mentioned algorithms has shown efficiency increasing up to 60 %, further investigations of applicability should be continued. In manuscript [7], inductive motor flux was regulated by using Artificial Neural Network control algorithm that indicates satisfactory efficiency results of 18 % for motor operation under steady state conditions. However, the applied control technique was unable to degrade energy losses when the motor was loaded less than 60 % of rated load. In study [13], power loss in induction motor was decreased up to 50 % by controlling the flux by using Genetic Algorithm and Fuzzy Genetic Algorithms in programmable logic controller (PLC).
Additional power losses occur in the working transferring systems, such as valves and pipes. Moreover, efficiency optimization methods that were described above require a lot of mathematical calculations and technically sophisticated equipment. Additionally, the programmable equipment has to be reinstalled for every new use of controlling algorithm. All these disadvantages make hard to provide an efficiency optimization probe in the specific VDF. Thus, the new investigations in the VDF efficiency optimization are important and still extremely relevant.

Modern scientific research paid insignificant attention to the automation systems equipped by VDF and their efficiency analysis, evaluation, and optimization [20]. Authors state that nowadays there is no unified and satisfactory method for motor’s efficiency evaluation used everywhere in the automated industry. Most automation systems are arranged by VFDs that are operating in periodical modes. It means that motors in the VFD operate in the defined duty or load cycles. Generally, transporting equipment of packages includes several VFD drives that operate with different duty cycles. To increase energy consumption of the described automation system, it was decided to extend the stop times of motors because the motor duty cycle includes the ratio of running time to the sum of running and stopping times. Operational time duration of all system’s constituents was measured using computer software. The stop time duration was obtained from different types of packages within two hours of incessant operation of the automation line using a programmable logic controller that was connected to each drive of equipment. The electricity expenditures were measured by connecting the measuring leads to the feeders of induction motors, variable frequency drives, and the feeder of servo drive’s controller. This was done when the heaviest package was transferred to evaluate the energy consumption under the condition of largest motor’s load.

Duration of each cycle step was measured separately from the others by running motors in automated modes and returning them to the initial position manually.

Load cycle of the motor is the main VDF parameter that allows reaching the best efficiency. Duty cycles of each motor consist of drive run and stop times that vary periodically [14]. The duration of run and stop times is different and depends on the aims of technological process to be done by the system [15]. The cyclical operation of motor in the periodically repeating stop/run modes allows managing the load on the motor shaft that leads to VDF efficiency, which increases because during motor stop time the power is not consumed by motor from the grid [16].

Presented study focuses on the VFD optimization based on the changes of motor load cycles, as well as finding optimal frequencies and linear speed of automated industrial system drives. The suggested method is based on obtaining the optimal VFD parameters and applying them in the existing drive equipment without any changes in drive constituents. From this point of view, the results of presented study can be useful for practical application in the similar automation systems for their adjustment and performance improvement.

The most important parameter of efficiency for the automated industry processes is manufacturing lead-time [17] that is one cycle duration of the packages’ transfer line.

In industrial automation systems, the OEE index, known as the multiplication of Availability, Performance, and Quality, shows the efficiency of manufacturing. In this formula, the Performance is the division of Ideal Cycle Time and Real Cycle Time. According to [19], most manufacturing companies have an OEE score between 40 % and 60 %. The authors concluded that performance ratio depends on machine operating cycles. Therefore, practical aspects for the VFD system settings described in this paper are of current interest and benefit.

The optimal frequency and voltage for the motor found by some studies [18], [20] offer simulation models based on the complicated mathematical calculations and elaborate the design of models using MATLAB/SIMULINK software. Also, induction motor [18] was tested in laboratory conditions that cannot be compared to real conditions of the compound operating motor system with VFD. The proposed model [20] requires additional testing and VFD settings correction in order to use it in real life industrial systems.

In comparison to suggested methods in [18], [20] for obtaining optimal frequency and optimal linear speed of motor, frequencies and linear speed values were calculated at first. Each step was increased by 10 %, starting from 40 % of the initial speed value up to 100 % using simple arithmetic equations. At the second stage, the system was operated by obtaining frequency and linear speed values and measuring energy consumption under these conditions. The optimized frequency and linear speed parameters correspond to lower energy consumption by the motors. In the third step, linear equation systems evaluating energy consumption depending on the step time duration were composed in order to precise the optimized cycle duration. MATLAB software that is widely used in the scientific world was utilized to solve the equation systems. Hence, suggested methods for the efficiency optimization in industrial automated systems arranged with VFD are implemented effortlessly and provide a noticeable electricity expenditure reduction.

II. SYSTEM STRUCTURE AND PRINCIPLE OF OPERATION

Package transportation automation line includes electric motors and frequency converters, and operates in cycle regime. The rated constants for these motors and frequency converters are presented in Table 1. Each cycle includes 10 steps, which vary in length. The motors of system’s electric drives operate at maximum speed and 50 Hz rate frequency. The capture pitchforks of the lifting mechanism move with maximum permitted speed of 0.2 m/s. The constituents of the system are shown in Fig. 1, and the operating guiding principle is described below.

In the conventional start of the cycle, the pitchforks 7 are normally raised, cart 3 is near a supplying conveyor 1, and all electrical drives (M1, M2, and M3) are stopped. When the sensor indicates the package presence on the supplying conveyor, the rollers 6 driven by motor M1 start to rotate CW direction that results in package motion to the cart.

After the package is completely placed on the cart surface, the M1 motor is switched off and the cart wheels’ 4 drive M2 is switched on to allow transportation of the 1st package by the cart moving on rails 5 toward storehouse conveyor 8.
The cart’s forward motion towards the storehouse conveyor is stopped when the safety distance is achieved between cart and lifting mechanism of pitchforks.

![Diagram of package transportation system]  

**Fig. 1. The complex structure of package transportation: 1 – Supplying Conveyor (SC); 2 – Package; 3 – Cart; 4 – Cart Wheels; 5 – Rails Track; 6 – Rollers; 7 – Pitchforks of Lifting Mechanism (PLM); 8 – Warehouse Conveyor (WC); M1 – Rollers drive motor; M2 – Motor of cart wheel drive.**

This distance is indicated by a sensor and initiates the stop of M2 electric machine, as well as of the cart 3. In the following step, the motor M3 of Pitchforks’ Lifting Mechanism starts to operate and the capture pitchforks are lowered to pick up the 1st package. The M2 motor gets a signal from height measuring sensor and cart with the 1st package moves toward the lifting mechanism. At this moment, M2 motor rotates in CCW direction. The cart stops in such a position near the lifting mechanism that the pitchforks are placed underneath the 1st package. At this moment, the M2 machine of cart wheels stops. After that, the M3 starts to run and the procedure is repeated: M1 electric motor starts to rotate the rollers CW and the 2nd package is moved to the surface of cart. When the 2nd package completely covers the cart surface, the lifting mechanism starts to operate again dropping the 1st package onto the 2nd one. When the 1st package is successfully placed on the 2nd, the M3 machine of lifting mechanism is stopped. Finally, the M2 motor of cart wheels starts rotating CW to move two packages by rails toward warehouse conveyor.

In order to investigate the influence of stop time duration to efficiency of system, the continuance of each cycle step was measured. The cycle steps, as well as their length-time, are presented in Table II.

**TABLE II. OPERATION ALGORITHM AND ITS STAGES DURATION.**

<table>
<thead>
<tr>
<th>Part of cycle</th>
<th>1st part</th>
<th>2nd part</th>
</tr>
</thead>
<tbody>
<tr>
<td>Step No.</td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>Operation description</td>
<td>1st package is moving into cart</td>
<td>Cart moves with 1st package toward WC</td>
</tr>
<tr>
<td>Duration, s (actual)</td>
<td>5.1</td>
<td>5.1</td>
</tr>
<tr>
<td>Total duration of cycle, s</td>
<td>76</td>
<td></td>
</tr>
</tbody>
</table>

**TABLE I. THE EQUIPMENT DRIVES’ RATED PARAMETERS.**

<table>
<thead>
<tr>
<th></th>
<th>Motor</th>
<th>Frequency converter</th>
<th>Motor</th>
<th>Frequency converter</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roller drive (M1)</td>
<td>SEW-EURODRIVE R37 M3</td>
<td>Delta VFD015E43A</td>
<td>Kollmorgen</td>
<td>Kollmorgen</td>
</tr>
<tr>
<td>Cart wheel drive (M2)</td>
<td>DR571M4</td>
<td></td>
<td>AKM53K-NC2R-00</td>
<td>AKD-P01206-NBCC-E00</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Parameter</th>
<th>Value</th>
<th>Parameter</th>
<th>Value</th>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Frequency, Hz</td>
<td>50</td>
<td>Voltage, U (3-phs)</td>
<td>380–480</td>
<td>Current (RMS), A</td>
<td>9.1</td>
<td>Input voltage, V</td>
<td>120(1-phs)/240(3-phs.)</td>
</tr>
<tr>
<td>Rotating speed, rpm</td>
<td>1342</td>
<td>Input current, A</td>
<td>4.3</td>
<td>Max. rotating speed, rpm</td>
<td>4500</td>
<td>Output voltage, V</td>
<td>0–240</td>
</tr>
<tr>
<td>Power, kW</td>
<td>0.55</td>
<td>Power, kW</td>
<td>2 (≈ 1.5 kW)</td>
<td>Power, kW</td>
<td>1.06</td>
<td>Input frequency, Hz</td>
<td>50/60</td>
</tr>
<tr>
<td>Voltage, U (Y)</td>
<td>380–420</td>
<td>Output current, A</td>
<td>4.2</td>
<td>Max. torque, Nm</td>
<td>11.25</td>
<td>Output frequency, Hz</td>
<td>0–800</td>
</tr>
<tr>
<td>Current, A</td>
<td>1.62</td>
<td>Output frequency, Hz</td>
<td>0.1–600</td>
<td>Current (RMS), A</td>
<td>12</td>
<td>Power, kVA (240 V)</td>
<td>3.82</td>
</tr>
<tr>
<td>PF</td>
<td>0.72</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
It was discovered that during system operation after completing cycle steps, system stops and waits while the Supplying Conveyor will deliver a new package. In ideal operation mode, the package is placed on the cart straight away after it was put on the Supplying Conveyor.

However, under real conditions the cart is in the stopped mode. It was noticed that the cart stops its movement between 10th and 1st step of cycle when the 1st package is placed on the cart, as well as between 5th and 6th stages of cycle when the 2nd package is placed on the cart.

The stop time, as it is shown in Table III, varies due to the working conditions of the previous automated line equipment and additionally depends on the transported package weight.

Some type of packages are delivered faster compared to the others. The lower the speed of drives, the smaller electrical energy expenditure.

### TABLE III. STOP TIME DURATION DEPENDENCY ON PACKAGE TYPE.

<table>
<thead>
<tr>
<th>Package type</th>
<th>Type 1</th>
<th>Type 2</th>
<th>Type 3</th>
<th>Type 4</th>
<th>Type 5</th>
<th>Type 6</th>
</tr>
</thead>
<tbody>
<tr>
<td>( t_{\text{max}} ) (s)</td>
<td>41.1</td>
<td>54.1</td>
<td>62.0</td>
<td>81.3</td>
<td>100.3</td>
<td>160.6</td>
</tr>
<tr>
<td>( t_{\text{min}} ) (s)</td>
<td>119.2</td>
<td>159.5</td>
<td>196.1</td>
<td>157.7</td>
<td>198.7</td>
<td>256.7</td>
</tr>
<tr>
<td>( t_{\text{average}} ) (s)</td>
<td>79.2</td>
<td>105.5</td>
<td>136.0</td>
<td>119.0</td>
<td>159.1</td>
<td>205.3</td>
</tr>
</tbody>
</table>

Therefore, it was concluded to obtain the precise stop time of the system drives and to harmonize operating mode duration in such a way that system’s equipment operation would be slowed down, so that it would result in the increase of the total system efficiency.

### III. FINDING OF OPTIMAL PARAMETERS

As it is shown in Table II, without including the duration time between the cycle two parts: the first part (between 1st and 10th steps) and the second part (between 5th and 6th steps) of operation cycle are equal to 76.0 s. It can be seen that 8th, 9th and 10th time duration steps constitute to more than half of the whole cycle time, i.e., it is a time that includes cart moving time toward Storage Conveyor, package shifting from cart to SC surface and returning. According to Table III, the average smaller stop time needed to prepare package to be shifted onto cart surface is 79.2 s (“Type 7”), while the biggest average time is obtained for package “Type 6” when average stop time is equal to 205.3 s.

Taking into account the possible operational faults, the optimized automation unit operation cycle should be calculated as

\[
 t_C = t_{av} \times k_s, \quad (1)
\]

where \( t_C \) is the optimized cycle duration, [s]; \( t_{av} \) is the average stop time between two parts of cycle, [s]; \( k_s \) is the spare 10 % factor applied for the possible operational faults, %.

The continuances of the first and second cycle parts are obtained as follows:

\[
 t_I = \sum_{i=1}^{n=5} t_i, \quad (2)
\]

where \( t_I \) and \( t_{II} \) – the duration of the first and the second cycle parts, respectively, [s]; \( i \) is duration value corresponding to the \( i \)th step of the cycle, [s]; \( n \) is the number of steps in the cycle part.

Therefore, taking into account that the first cycle part (from 1st to 5th step) of considered equipment is accomplished during 30.3 seconds, the average stop times of 1st stand of the 2nd cycle part are calculated as:

\[
 t_{s(I)} = t_C - t_I, \quad (4)
\]

\[
 t_{s(II)} = t_C - t_{II}, \quad (5)
\]

where \( t_{s(I)} \) and \( t_{s(II)} \) are the average stop times over the first and second cycle parts accordingly, [s].

The total stop time over two cycle parts is obtained as

\[
 t_s = t_{s(I)} + t_{s(II)}. \quad (6)
\]

Hence, the optimized duty cycle of considered automation system is expressed in percentage and evaluated

\[
 t_{DT} = \frac{t_{s(I)} + t_{s(II)}}{t_{I} + t_{II} + t_{s(I)} + t_{s(II)}} \times 100\%. \quad (7)
\]

Operational times of system equipment cycles obtained using equations (1)-(7) are presented in Table IV. The equipment velocities of previous automation line could not be accelerated as they operate on the maximum speed. Therefore, operational time of the cart and pitchforks drives can be extended to 45.6 % without any influence for system operation, i.e., duration time of each cycle part can be extended up to 71 s.

### TABLE IV. CYCLES AND THEIR STOP TIME DURATION.

<table>
<thead>
<tr>
<th>( t_{C1} ) (s)</th>
<th>( t_{I1} ) (s)</th>
<th>( t_{I2} ) (s)</th>
<th>( t_{I3} ) (s)</th>
<th>( t_{II1} ) (s)</th>
<th>( t_{II2} ) (s)</th>
<th>( t_s ) (s)</th>
<th>( t_{DT} ) (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>71</td>
<td>30.3</td>
<td>45.7</td>
<td>40.7</td>
<td>25.3</td>
<td>66</td>
<td>46.5</td>
<td></td>
</tr>
</tbody>
</table>

The energy consumption was measured for each \( n \)th step of the cycle by changing operation speed of drives. The speed for electrical machines was slowed by increasing deceleration factor which value was changed by increasing each step by 10 %, starting from 40 % of the initial speed value up to 100 %. The equations used for the installing frequency and linear speed calculation are presented below

\[
 f_n = f_0 \times \frac{t_{n0}}{t_n}, \quad (8)
\]

where \( f_n \) is VFD \( n \)th step frequency, [Hz]; \( f_{n0} \) is drive’s initial frequency, [Hz]; \( t_n \) is the \( n \)th step of cycle duration time for linear motion of pitchforks, [s]; \( t_{n0} \) is \( n \)th step actual time values presented in Table II.

\[
 v_n = v_{n0} \times \frac{t_{n0}}{t_n}, \quad (9)
\]
where \( v_n \) is \( n^{th} \) step linear speed, [m/s]; \( v_{n0} \) is initial linear speed, [m/s].

Set up parameters obtained from (8) and (9) are presented in Table V and Table VI. Their values were used for the measurement of electricity consumption by the system drives in both operation cycle parts. The frequencies of motors’ drives, as well as linear speed, were changing according to data shown in Table V and Table VI and for 1\textsuperscript{st} and 2\textsuperscript{nd} cycle part, respectively. For every speed value, the energy utilization measurements were done twice. Therefore, there were 14 measurements for every cycle step.

Measurement readings were loaded to the Matlab software, and electricity consumption graphics were drawn for both cycle parts as shown in Fig. 2 and Fig. 3, respectively.

### TABLE V. ADJUSTABLE PARAMETERS FOR THE ENERGY CONSUMPTION METERING OF DRIVES (PART I OF CYCLE).

<table>
<thead>
<tr>
<th>Step</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>( k_d )</td>
<td>( f_t ) (Hz)</td>
<td>( t_{v} ) (s)</td>
<td>( f_t ) (Hz)</td>
<td>( t_{v} ) (s)</td>
<td>( f_t ) (Hz)</td>
</tr>
<tr>
<td>40 %</td>
<td>20</td>
<td>12.75</td>
<td>20</td>
<td>15.25</td>
<td>0.08</td>
</tr>
<tr>
<td>50 %</td>
<td>25</td>
<td>10.20</td>
<td>25</td>
<td>12.20</td>
<td>0.10</td>
</tr>
<tr>
<td>60 %</td>
<td>30</td>
<td>8.50</td>
<td>30</td>
<td>10.17</td>
<td>0.12</td>
</tr>
<tr>
<td>70 %</td>
<td>35</td>
<td>7.29</td>
<td>35</td>
<td>8.71</td>
<td>0.14</td>
</tr>
<tr>
<td>80 %</td>
<td>40</td>
<td>6.38</td>
<td>40</td>
<td>7.63</td>
<td>0.16</td>
</tr>
<tr>
<td>90 %</td>
<td>45</td>
<td>5.67</td>
<td>45</td>
<td>6.78</td>
<td>0.18</td>
</tr>
<tr>
<td>100 %</td>
<td>50</td>
<td>5.10</td>
<td>50</td>
<td>6.10</td>
<td>0.20</td>
</tr>
</tbody>
</table>

### TABLE VI. ADJUSTABLE PARAMETERS FOR THE ENERGY CONSUMPTION METERING OF DRIVES (PART II OF CYCLE).

<table>
<thead>
<tr>
<th>Step</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>( k_d )</td>
<td>( f_t ) (Hz)</td>
<td>( t_{v} ) (s)</td>
<td>( f_t ) (Hz)</td>
<td>( t_{v} ) (s)</td>
<td>( f_t ) (Hz)</td>
</tr>
<tr>
<td>40 %</td>
<td>20</td>
<td>12.50</td>
<td>20</td>
<td>3.25</td>
<td>0.08</td>
</tr>
<tr>
<td>50 %</td>
<td>25</td>
<td>10.00</td>
<td>25</td>
<td>2.60</td>
<td>0.10</td>
</tr>
<tr>
<td>60 %</td>
<td>30</td>
<td>8.33</td>
<td>30</td>
<td>2.17</td>
<td>0.12</td>
</tr>
<tr>
<td>70 %</td>
<td>35</td>
<td>7.14</td>
<td>35</td>
<td>1.86</td>
<td>0.14</td>
</tr>
<tr>
<td>80 %</td>
<td>40</td>
<td>6.25</td>
<td>40</td>
<td>1.63</td>
<td>0.16</td>
</tr>
<tr>
<td>90 %</td>
<td>45</td>
<td>5.56</td>
<td>45</td>
<td>1.44</td>
<td>0.18</td>
</tr>
<tr>
<td>100 %</td>
<td>50</td>
<td>5.00</td>
<td>50</td>
<td>1.30</td>
<td>0.20</td>
</tr>
</tbody>
</table>

Using trend lines (Fig. 2 and Fig. 3) obtained during system operation simulation under different frequencies and velocity values, the equation systems were composed that evaluate energy consumption dependency on the step time duration for the both cycle parts:

\[
E_1 (t_1) = 0.0069t_1^2 - 0.202t_1 + 1.89, \\
E_2 (t_2) = 0.0041t_2^2 - 0.172t_2 + 2.21, \\
E_3 (t_3) = 0.000030t_3^2 - 0.0040t_3 + 0.218, \\
E_4 (t_4) = 0.00660t_4^2 - 0.205t_4 + 2.08, \\
E_5 (t_5) = 0.00396t_5^2 - 0.175t_5 + 4.58,
\]

where \( t_1, t_2, \ldots, t_5 \) – the duration of 1\textsuperscript{st}, 2\textsuperscript{nd}, ..., 5\textsuperscript{th} step accordingly for cycle part I, [s]; \( E_1 (t_1), E_2 (t_2), \ldots, E_5 (t_5) \) – energy consumption at 1\textsuperscript{st}, 2\textsuperscript{nd}, ..., 5\textsuperscript{th} step accordingly, [Wh].

\[
E_6 (t_6) = 0.00546t_6^2 - 0.169t_6 + 1.71, \\
E_7 (t_7) = 0.00220t_7^2 - 0.016t_7 + 0.073, \\
E_8 (t_8) = 0.00137t_8^2 - 0.147t_8 + 4.79, \\
E_9 (t_9) = 0.00320t_9^2 - 0.163t_9 + 2.77, \\
E_{10} (t_{10}) = 0.00167t_{10}^2 - 0.140t_{10} + 3.90,
\]

where \( t_6, t_7, \ldots, t_{10} \) – the duration of 6\textsuperscript{th}, 7\textsuperscript{th}, ..., 10\textsuperscript{th} step accordingly for cycle part II, [s]; \( E_6 (t_6), E_7 (t_7), \ldots, E_{10} (t_{10}) \) – energy consumption at 6\textsuperscript{th}, 7\textsuperscript{th}, ..., 10\textsuperscript{th} step accordingly, [Wh].

Durations time with which the lowest amount energy is consumed were defined using equations:

\[
t_I = \sum_{i=1}^{n=5} \frac{t_i}{k_d}, \\
t_{II} = \sum_{i=6}^{n=10} \frac{t_i}{k_d}.
\]

Energy consumption during cycle parts I and II is calculated as follows:

\[
E_I = \sum_{i=1}^{n=5} E_i, \\
E_{II} = \sum_{i=6}^{n=10} E_i,
\]

where \( E_I \) and \( E_{II} \) – total energy consumed by system during cycle’s parts I and II, respectively, [Wh]; \( E_i \) is the amount of energy corresponding to the \( i^{th} \) step of the cycle, [Wh].

Total energy consumption during the cycle is

\[
E_C = E_I + E_{II}.
\]
As it was discussed previously, the maximum duration value of each cycle’s part should be in the range of 68 s–71 s. Following this condition, 757 and 7020 solutions (with resolution $R = 10$) and 2516 and 1669 solutions (with resolution $R = 50$) for the equation systems (10), (11) were obtained, respectively. All results are shown in Figs. 4–7. As it is shown in Fig. 4 and Fig. 6, under condition that $R = 10$, the obtained results are disposed within the range of 4.2 Wh–4.9 Wh and 4.0 Wh–6.5 Wh for cycle parts I and II accordingly. The ranges with the smallest electricity consumption are outlined by the red frame in the Fig. 4 and Fig. 6.

To achieve more precise results, the calculations were repeated by increasing the resolution to $R = 50$ and filtering all results greater than 4.2 Wh (for the part I) and greater than 4.3 Wh (for the part II). There were 2516 and 1669 results obtained which match with the given duration range of cycle parts.

IV. UTILIZED ENERGY QUANTIFICATION

More accurate calculations’ results (when $R = 50$) are shown in Fig. 5 and Fig. 7.
V. Discussion

It was determined that the lowest power consumption in either cycle part would be if the system was operated within time intervals, as well as with defined frequencies and linear speeds that are listed in Table VII.

TABLE VII. OPTIMISED SETTING PARAMETERS OF EQUIPMENT

<table>
<thead>
<tr>
<th>Cycle stage</th>
<th>Electric motor designation</th>
<th>Time ($t_s$), s</th>
<th>Frequency ($f_s$)</th>
<th>Linear speed ($v_s$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>M2</td>
<td>12.75</td>
<td>20 Hz</td>
<td>-</td>
</tr>
<tr>
<td>2</td>
<td>M1</td>
<td>15.25</td>
<td>20 Hz</td>
<td>-</td>
</tr>
<tr>
<td>3</td>
<td>M3</td>
<td>12.21</td>
<td>20 Hz</td>
<td>0.11 m/s</td>
</tr>
<tr>
<td>4</td>
<td>M1</td>
<td>13.75</td>
<td>20 Hz</td>
<td>-</td>
</tr>
<tr>
<td>5</td>
<td>M3</td>
<td>17.00</td>
<td>-</td>
<td>0.08 m/s</td>
</tr>
</tbody>
</table>

Total cycle’s part duration: 70.96

<table>
<thead>
<tr>
<th>IIInd part of cycle</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cycle stage</td>
</tr>
<tr>
<td>6</td>
</tr>
<tr>
<td>7</td>
</tr>
<tr>
<td>8</td>
</tr>
<tr>
<td>9</td>
</tr>
<tr>
<td>10</td>
</tr>
</tbody>
</table>

Total cycle’s part duration: 70.97

These optimized frequencies and linear speeds were obtained using (8), (9).

Optimized parameters, presented in Table VII, were applied to the equations (10) and (11) systems that allow to define the values of minimums of electrical energy consumption in the system during the cycle.

The comparative values of the system energy consumption before and after optimization are shown in Table VIII.

TABLE VIII. OPTIMISED SETTING PARAMETERS OF EQUIPMENT

<table>
<thead>
<tr>
<th>Energy expenditures measurements, (Wh)</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>Average value</th>
</tr>
</thead>
<tbody>
<tr>
<td>After optimisation</td>
<td>8.83</td>
<td>8.52</td>
<td>8.79</td>
<td>8.71</td>
</tr>
</tbody>
</table>

Calculated value 8.51

It was found that if the first cycle part duration would be 70.96 seconds, the system would operate consuming 4.21 Wh of energy per cycle. Also, if the operational time of the second part cycle would be 70.97 s, the system would consume 4.22 Wh of energy per cycle.

The total energy consumption during operational time was calculated using (16), System parameters were reinstalled using data shown in Table VIII, newly obtained data and the energy consumption were measured.

VI. Conclusions

The efficiency of industrial processes’ energy consumption decreases by monitoring, measuring, and optimizing system parameters, such as frequency of electrical drive and its linear speed. The optimization of these parameters allows saving about 60 % of energy per cycle.

During this study, it was found that 46.5 % of operational time is uselessly wasted when waiting for the next package, and it was calculated that the operational time of each of two cycle parts could be extended to 71 s. It was obtained that in order to improve efficiency the system should complete the first part of the cycle in 70.96 s and consume 4.21 Wh of electricity. The second part of the cycle should be completed in 70.97 s and consume 4.22 Wh of electricity. The optimized power consumption of the system is 8.51 Wh per cycle. The estimated average power consumption of a newly set system is 8.71 Wh, which is only 2.4 % error of mathematical calculations’ results in comparison with measured power values. The method provided in this study is applicable as a good practice to investigate other industrial processes.

CONFLICTS OF INTEREST

The authors declare that they have no conflicts of interest.

REFERENCES


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