Research of the Usage of Double-fed Generators in Wind Turbines

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Introduction

Many predictions say that rather soon wind energy will become one the main sources for power production in global scale [1]. Presently Lithuania has installed only less than 60 MW of cumulative wind turbines’ capacity and is lagging behind in comparison with many other countries. Rapid progress of the wind power development in this country restrict local bureaucratic barriers on the way of access to the electric grid, lack of the more favourable legal basis, potential problems of wind origin power balancing and reservation in the power grid, low and moderate wind energy resources in some regions located farther to the east from the seaside, lack of the financial means and some other.

The best wind energy resources are in the Baltic Sea and in approximately 30-50 km width stripe along the sea shore. Industrial generation of power in the wind farms is the most purposeful in this region. Wind turbines (WT) of small and medium scale can be installed in the best sites in other regions of the country. They can operate in stand-alone or grid-connected mode. Anyway, the better option would be the grid-tied operation just because the usage of expensive batteries for power storage is not necessary in this case.

The simplest scheme of wind energy conversion into the electric power is in case when the squirrel cage motor is used for operation in the generator’s mode. This way of wind energy conversion was used rather often at the beginning of the wind power development. However, this power conversion system can operate efficiently only at high wind speeds. The stand-alone mode of operation is possible in this case but the grid-connected option is more reliable and more efficient.

Synchronous generators are used in wind energy conversion systems in both modes of operation: stand-alone and grid connected. The synchronous generator can be connected into the power grid directly or over the grid-tied inverter [2].

Reasoning of the wind energy conversion system with double-fed generator

Currently double fed asynchronous machines (DFM) often are used in the WT of large capacity (700-3000 kW). Circuits of rotor of the DFM are connected with power grid over the converters. Usually such system of wind energy conversion operates well enough, however only at high wind speeds (8-15 m/s) [2]. Additionally, the converter used for the connection of rotor circuit with power grid is rather expensive. Therefore it would be purposeful to research a simplified scheme for wind energy conversion in WT capacity 50-250 kW where the DFM operates like the asynchronous motor working in dynamic braking mode. Stator circuit of the DFM is fed by the DC from the AC/DC converter in order to excite the generator. Rotor circuit of the DFM is connected with power grid over the inverter as it is shown in Fig. 1.

Fig. 1. Simplified electrical scheme of WT with DFM
Another peculiarity of this wind energy conversion scheme is the power storage circuit SC inserted in the power conversion chain between the rectifier and the inverter.

As it is shown in Fig. 1, the stator circuit of DFM is exited by the non-controlled rectifier U, which is connected to the electric grid through the switch Q, F. The rotor circuit of DFM is connected to the electric grid through the rectifier, the shorting and energy storage circuit SC, the inverter and the switch Q. The circuit has the shorting transistor V and the power storing elements Ld and Ck.

Wind turbine’s control system changes the angle of inversion (by means of inverter’s pulse former IPF) and the width of shorting pulse (by means of shorting circuit pulse former SCPF) depending on the shaft’s rotational speed \( \omega_g \), and, therefore, simultaneously changes the quantity of energy stored in the reactor \( L_d \). The active and reactive energy, supplied into electric grid from the WT, changes dependently on this angle and pulse width.

Power supply into electric grid from the wind power conversion system (Fig. 1) can be controlled within period of 10 milliseconds. When the shorting circuit is used, amount of the reactive power supplied or taken from the grid can be controlled. It depends on the inverting and shorting angles with respect to the grid voltage phase.

Mathematical description and model of the WT’s power circuits

Further going researches will be based on the mathematical description and model of the proposed WT’s power conversion system. Firs of all it will be performed for the power circuits. The equivalent scheme of the DFM shown in Fig. 2 will be used for this purpose [3].

![Fig. 2. Equivalent scheme of the generator](image)

Usually the stator’s windings are fed by the DC current \( I_1 \), which is close to the rated AC current \( I_N \) in order to create the proper exciting flux. The exciting current \( I_1 \) can be defined more exactly by using the following formulas [3]:

\[
I_1^2 = I_2^2 + 2I_\mu \cdot I_2 \cdot \sin \phi_2 + I_\mu^2,
\]

\[
\sin \phi_2 = \frac{x_2^2}{\sqrt{x_2^2 + y_2^2}},
\]

where \( I_1 \) - the exciting current; \( I_\mu \) - the magnetizing current; \( I_2 \) - the reduced current of the rotor; \( x_2 \), \( y_2 \) - the reduced active and inductive resistances of the rotor.

The ratio of generator’s angular speed and its no load angular speed \( s \) is calculated as follows:

\[
s = \frac{\omega_g}{\omega_{g0}},
\]

where \( \omega_g \) is the angular speed of the generator; \( \omega_{g0} \) – the angular synchronous speed of the generator.

The following simplified formula is mostly used for calculation of the exciting current \( I_2 \):

\[
I_2 = I_N \cdot \sqrt{3} \cdot \cos 30^\circ = 1.22 \cdot I_N.
\]

The necessary voltage of the DC power source for feeding of the exciting circuit is calculated according to this formula:

\[
U_2 = 2 \cdot r_1 \cdot I_2,
\]

where \( r_1 \) – the active resistance of the generator’s stator winding.

Voltage of the DFM generated in the rotor’s windings \( E_2 \) is calculated as follows:

\[
E_2 = E_{2N} \cdot s,
\]

where \( E_{2N} \) – the rated delta voltage of rotor (at \( s=1 \)).

The generator is loaded through the rectifier. The rectified parameters of the DFM can be calculated by formulas presented in previous authors’ publication [4]. The rectified internal voltage of the generator can be calculated by using the formula:

\[
e_{g0} = \frac{2\sqrt{2} \cdot m \cdot E_{2f} \cdot \sin \frac{2 \cdot \pi}{m} \cdot \sin \frac{\pi}{m}}{\pi}.
\]

Phase voltage of the generator’s rotor can be expressed as this:

\[
E_{2f} = \frac{k_e \cdot \omega_g}{\sqrt{3}},
\]

where

\[
k_e = \frac{E_{2N}}{\omega_{g0}}.
\]

Effective phase current of the generator’s rotor depends on the rectified current and on the angle of commutation:

\[
I_{2f} = I_d \cdot \sqrt{\frac{2 - \gamma}{3 \cdot \pi}}.
\]

The diodes’ commutation angle \( \gamma \) can be calculated by using this formula:

\[
\gamma = \arccos \left( 1 - \frac{\sqrt{2} \cdot x_K \cdot I_d}{U_2} \right).
\]

Voltage drop due to the commutation of rectifier’s diodes \( u_K \) can be described by the following expression:
\[ u_K = \frac{m}{2\pi} x_K \cdot I_d \cdot \] (12)

where in formulas (8)-(12) \( E_{2f} \) – the effective phase voltage of the rotor’s open circuit; \( m \) – the number of pulsations of the rectified voltage; \( U_g \) – the effective delta voltage of the rotor; \( k_e \) – factor of the rotor’s internal voltage; \( \omega_{eh} \) – the angular speed of the rotor; \( x_K \) – the inductive reactance of the diodes commutation; \( I_d \) – the rectified current; \( \gamma \) – the commutation angle of the diodes.

It can be admitted for the evaluating calculations that \( x_K \approx x_2 \) (\( x_2 \) – the inductive reactance of rotor’s phase).

Mathematical descriptions of the electromagnetic processes taking place in the converter’s power circuits have been made by using the simplifications well known in theory of converters’ circuits [4, 5, 6]. So the \( n \)-phase circuits of converter will be substituted by the one-phase equivalent scheme. Power switches will be considered as ideal.

One-line scheme of the researched WT circuitry is shown in Fig. 3.

![Fig. 3. Equivalent scheme of the wind turbine’s power circuits](image_url)

As it is shown in previous works of authors [4, 5, 7] the DFM generator (Fig. 3) operates in the two basic modes: shorting mode – when the switch \( S_1 \) is closed, and power inverting mode – when the switch \( S_2 \) is opened and switch \( S_1 \) is closed. When the generator is operating in the shorting mode (\( S_1 \) – OFF, \( S_2 \) – ON) its power circuits can be described as follows:

\[
\begin{align*}
\frac{di_d}{dt} &= \frac{1}{L_d}(u_g - r_d \cdot i_d); \\
u_d &= e_{g0} - u_g - u_K; \\
u_g &= \frac{2 \cdot r_d \cdot i_d + 2 \cdot L_2 \cdot \frac{di_d}{dt}}{2}; \\
u_K &= \frac{m \cdot x_K}{2 \cdot \pi} \cdot i_d; \\
\end{align*}
\] (13)

where \( u_g \) – the voltage of the generator; \( i_d \) – the rectified current of the generator; \( r_d \) – the active resistance of the generator; \( r_f \) – the active resistance of the reactor; \( L_2 \) – the inductance of the generator; \( L_d \) – the inductance of the reactor.

When the switch \( S_1 \) is switching off and the switch \( S_2 \) does not switched on yet the generator power circuits can be described as follows:

\[
\begin{align*}
\frac{di_d}{dt} &= \frac{1}{L_d}(u_g - r_d \cdot i_d); \\
u_d &= e_{g0} - u_g - u_K; \\
u_g &= \frac{2 \cdot r_d \cdot i_d + 2 \cdot L_2 \cdot \frac{di_d}{dt}}{2}; \\
u_K &= \frac{m \cdot x_K}{2 \cdot \pi} \cdot i_d; \\
\end{align*}
\] (14)

where \( E_{im} \) – the maximum value of the grid’s delta voltage; \( u_g \) – the voltage of the rectifier’s scheme.

When the generator is operating in the inverting mode (\( S_1 \) – OFF, \( S_2 \) – ON) its power circuits can be described by means of the system of differential and algebraic equations as follows:

\[
\begin{align*}
\frac{di_d}{dt} &= \frac{1}{L_d}(u_g - u_{ab} - r_d \cdot i_d); \\
u_d &= e_{g0} - u_g - u_K; \\
u_g &= \frac{2 \cdot r_d \cdot i_d + 2 \cdot L_2 \cdot \frac{di_d}{dt}}{2}; \\
u_K &= \frac{m \cdot x_K}{2 \cdot \pi} \cdot i_d; \\
u_{ab} &= U_{e0} + r_k \cdot i_k; \\
i_k &= i_k + i_k; \\
\end{align*}
\] (15)

where \( e_{g0} \) – the counteracting electromotive force of the grid; \( r_f \) – \( r_f \) – the active resistance of the inverter circuit; \( r_d \) – the active resistance of the grid; \( r_f \) – the active resistance of the filter; \( L_2 = L_1 + L_f \) – the inductance of the inverter’s circuit; \( L_1 \) – the inductance of the electric grid; \( L_2 \) – the inductance of the filter; \( i_k \) – the inverted current.

When the switch \( S_1 \) is in the position OFF and the switch \( S_2 \) is just after the switching off, the generator power circuits can be described by using system of equations 15 with some modifications: \( e_{g0} = 0 \) and current \( i_k = i_k \) (see Fig 3.3).

When the switch \( S_1 \) is in the position ON and the switch \( S_2 \) is just after the switching off, the generator power circuits can be described as follows:
\[
\begin{align*}
\frac{di_t}{dt} &= \frac{1}{L_t}(u_{ab} - r_i \cdot i_t), \\
\frac{du_c}{dt} &= \frac{1}{C_k} i_k; \\
u_{ab} &= U_c + r_k \cdot i_k; \\
i_k &= i_v = i_l. \\
\end{align*}
\]

(16)

Mechanical part of the DFM can be described like it was done in the papers [4, 7]:

\[
\begin{align*}
\frac{d\omega_g}{dt} &= \frac{1}{J}(T_{tg} - T_g - T_f), \\
T_{tg} &= \frac{P_t}{\omega_l \cdot i}; \\
T_g &= k_w \cdot I_l; \\
T_f &= k_f \cdot \omega_l; \\
\end{align*}
\]

(17)

where \(T_g\) – the torque of generator; \(T_{tg}\) – the torque of wind turbine shaft calculated to the generator’s rotor; \(T_f\) – the combined torque of viscous friction of rotor and load; \(J\) – the combined inertia of rotor and load; \(i\) – reduction (multiplication) factor of the gear; \(\omega_l\) – the angular velocity of the wind turbine shaft; \(\omega_k\) – the angular velocity of the generator’s rotor; \(k_w\) – torque factor; \(k_f\) – friction factor; \(P_t\) – the power produced by the wind turbine.

Characteristics of wind turbines

Wind turbines can be described by means of non-dimensional dependences of the power coefficient \(c_p\) on the tip-speed ratio \(\lambda\). Coefficient \(\lambda\) can be calculated by using this formula:

\[
\lambda = \frac{R \cdot \omega_w}{v_w},
\]

(18)

where \(R\) is the radius of wind rotor; \(\omega_k\) – the angular velocity of wind turbine rotor; \(v_w\) – the wind speed.

The power coefficient \(c_p\) for the wind turbine under research can be approximated as follows:

\[
c_p = -2.463e - 5 \cdot \lambda^7 + 6.6718e - 4 \cdot \lambda^6 - 0.006942 \cdot \lambda^5 + 0.0339 \cdot \lambda^4 - 0.0778 \cdot \lambda^3 + 0.08049 \cdot \lambda^2 - 0.0296 \cdot \lambda + 0.0063.
\]

(19)

The mechanical output power \(P_t\) at the shaft of the wind turbine can be calculated as follows [8]:

\[
P_t = \frac{1}{2} \cdot \rho \cdot c_p(\lambda) \cdot A \cdot v_w^3,
\]

(20)

where \(\rho = 1.225 \text{ kg/m}^3\) is the air density; \(A = \pi R^2\) – the swept area of the wind rotor.

The torque \(T_l\) at the shaft of the wind turbine can be calculated as follows:

\[
T_l = \frac{P_t}{\omega_l},
\]

(21)

Dependences of the wind turbine torque \(T_l\) on the angular velocity \(\omega_l\) when the wind speed \(v_w\) is constant are given in Fig. 4. The thicker line in the same figure shows the optimal load torque defined for the generator of the researched wind turbine. If load of the wind rotor will be controlled according to this curve, the wind turbine will supply into electric grid the maximal power, which value will depend only on the wind speed.

Fig. 4. Dependences of the wind turbine torque \(T_l\) on the angular velocity \(\omega_l\) when the wind speed is constant

The torque-speed characteristics are implemented in the torque signal forming (TSF) unit, which is shown in Fig.1. The value of the signal for reference the load torque of the wind turbine’s generator is calculated in the TSF unit accordingly to the measured angular velocity of the wind rotor. After this the current signal forming (CSF) unit calculates the value of the generator’s rectified current reference signal because load of generator is controlled by means of changing its rectified current. The rectified current is controlled by the pulse-width modulation by means of the shorting unit SC shown in Fig. 1.

Apart from the function of maximization of power produced by the wind turbine, the described control system has one more advantage: the system has a certain effect of filtration because it do not transmit into the control circuits any rapidly changing variations of the wind rotor’s power caused by the fluctuations of wind speed and aerodynamic harmonics of torque.

Mathematical model and simulation

Mathematical model of the researched wind turbine is shown in Fig. 5 and consists of the three main parts: double fed machine (DFM), wind turbine and storage and inverting circuits (SC and I).

Mathematical model for the DFM is made up using the systems of equations (13, 14, 15 and 17) as well as equations (1÷12). Mathematical model of the storage and inverting circuits is elaborated by application of the previously published works of authors [4, 5, 7].
Mathematical model of the wind turbine is based on the equations (18-21). The reference rectified current $I_r$ (Fig. 1) is calculated in the model’s block WT according to the formula presented in the previous paper of authors [4].

**Results of the WT’s operation research**

Wind turbine is purely non-linear object, which is described by the non-linear equations (18 ÷ 21 equations and system of equations 17). One of the best methods for research of this type of systems is the mathematical modelling and simulation. Therefore the researches of the proposed wind energy conversion system based on the double-fed machine were carried out by using of MATLAB/SIMULINK programme package. Duration of simulation depends on the time constants of the researched system’s blocks. When the inertia of wind rotor is large and the time constants of converter are small, the duration of simulation is long. Therefore in our case the initial terms were used in order to decrease the time of simulation: it was considered that wind turbine is rotating with angular velocity close to the steady value, which depends on the value of wind speed.

The quality of response of the wind turbine into the control signal and wind speed changes was performed by the simulation. Results of simulation are presented below in form of experimental curves.

The case when all power generated by the wind turbine is supplied into electric grid is researched. Results of researches of the WT operating are presented in Fig. 6. There is shown the process of operating WT when the load increases from zero to particular value and the wind velocity suddenly drops from 9 m/s down to 5 m/s. Initially wind turbine is switched on for operation in the idle mode. The load of wind turbine starts to increase only after 4 s. At first the load increases very slowly because the converter is operating in the mode of intermittent current without the power supply into electric grid. The converter starts to operate in the mode of continuous current approximately after 6.5 s. The power supply into electric grid begins and load power of the generator rapidly reaches the set value. As it can be seen in Fig. 6, the WT’s load control process is sufficiently qualitative.

Fig. 6. Curves of the WT’s power system parameters at the jump of generator’s load reference signal $U_l$ from 1 to 8 V after 4 s and drop of the wind speed $v_w$ from 9 to 7 m/s, at $t = 12$ s)

As we also can see in Fig. 6, after the wind speed drop the WT moves to another point of operation. After this the angular velocity and torque of the WT, the rectified current and power of the generator decreases. However, the form of the inverted current is not sinusoidal. Therefore the filters for the inverted current must be installed on output of the inverter.

**Conclusions**

1. Simplified grid-connected wind energy conversion system based on double-fed machine of moderate capacity is proposed.
2. Stator windings of the double-fed machine are fed by the DC from the AC/DC converter when rotor circuit of the machine is connected with power grid over the inverter.
3. Load of the wind turbine’s generator in the proposed energy conversion system is controlled dependently on the wind speed in order to maximize the energy output.
4. Control of the rectified current of double-fed machine and inverted current by the pulse-width modulation allows receiving a sufficient quality of wind turbine’s operation.
5. Mathematic model of the proposed wind energy conversion system with double-fed machine allows researching of the wind turbine’s dynamic properties.
6. Researches performed on basis of the mathematical model proved the necessity to increase the load of wind turbine slowly enough in order to avoid the considerable potentially harmful mechanical forces.
7. Research of the mathematical model of wind energy conversion system with double-fed machine confirmed the idea that using of the pulse-width modulator and control system for the wind turbine’s load control allows optimal controlling of the power supplying into electric grid depending on the wind speed.

References


Results of researches of the wind turbine with double-fed generator when its stator is fed from the DC power source are described in the paper. Usually stator and rotor of the wind turbine’s double-fed generator is connected with electric grid over the electronic converters. If capacity of wind turbine is not considerable, application of the generator’s exciting over the stator’s windings can be acceptable and justified in order of simplification of wind power conversion system. Only one converter is used in this case for connection of the rotor circuit with electric grid. Equivalent scheme and equations, which can be used for calculation of parameters of the power supplied into electric grid depending on the wind speed, are given in the paper. Electromagnetic processes for the intervals of operation, shorting and inverting are described by means of the system of differential equations. Mathematical model of the wind power conversion system is based on this system. Load of the wind turbine and pulse-width mode of operation of the inverter are taken into consideration. Results of the research showed the possibility to keep the wind turbine’s operation on the maximum available power depending on the wind speed. However, the inverted current has a pulse shape. Therefore the filters should be used after the inverter in order to make the inverted current closer to the sine wave. III. 6, bibl. 8 (in English, summaries in English, Russian and Lithuanian).


Strainspyne nagrinėjami dvigubo maitinimo generatorių naudojimo vėjo elektrinėse klausimai. Dažniausiai vėjo elektrinėse generatorių statoriaus ir rotorius jungiami su elektriniu tinkle naudojant puslaidininkinį setį. Daug paprasciau, ypač jeigu generatoriaus galia yra nedidelė, statorių ir rotorius maitinama direktyviniu srovė, o rotorius sujungtis su tinklu perklo inverteirą. Strainspyne pateikiamas tokios vėjo elektrinės ekvivalentinė schema ir lygtys, pagal kurias galima apskaičiuoti į elektros tinklą tiekiamos energijos parametrus, kai yra žinomas vėjo greitis. Generatoriaus galios grandinių elektromagnetinių procesai aprašytų taikant intervalų metodą. Visų darbo intervalų: trumpinimo, energijos kairės ir energijos atidavimo į tinklą elektromagnetiniai procesai aprašyti diferencialinių lygių sistemomis. Pagal šias lygių sistemų sudarytas matematinis modelis, kuriamo įvertinama vėjo turbinos apkovra, kai inverteris, jungiantis generatorius su elektros tinklu, dirba platuminio-impulsiniu režimu. Tyrimo rezultatai rodo, kad isitvirtintoje sistemėje visada galima palaikyti maksimali vėjo elektrinės apkovros galią, kurios vertė kinta priklausomai nuo vėjo greičio. Tačiau gaunama invertuojama srovė yra impulsinė, todėl būtina naudoti filtras, kad ši srove būtų artima sinusine. II.6, bibl. 8 (anglų kalba; santraukos anglą, rusų ir lietuvių k.).