Dynamic of a Rewinder with Feedback by Tension Force

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Introduction

Fundamental part of university education is to create connection of theoretical approaches with experimental or simulation methods for verification. Illustration of practical physical models is cardinal important for experimental exercises engineering, for comparing the computer simulation tasks with practical experiments and with real-time measured signals from technological aggregates. The improvement of theoretical findings is done by physical experimentation during the education process. The laboratory stands allow easy understanding of the various technologies and its control [7-10].

In most devices, technological process is performed by winding different types of materials. The most typical machines of this group are coiling machines in textile production, in the paper processing, wire making industry and etc. Technological process in these devices usually requires constant tension of the winded material (textile, paper, wires, threads and so on) at various velocities [1-5].

The universal stand of the winding band was design in department of control technologies at Kaunas University of Technology (Lithuania) for the educational and scientific purposes. The stand allows demonstrating and investigating the process of the winding band by controlling its tension in two ways. First method is done by measuring the diameter of unwinding roll or by measuring the length of the band loop. The second method is implemented by direct measurement of tension force of the band.

Fig. 1. Picture of the lab stand

Disadvantage of the first method is that it is able to ensure correct control of the tension force only in the stabilized case. Determining the tension by the dancer loop length, the length of the loop should be somehow measured by the distance meter. In this case, the length of the loop is proportional to the tension force; however the tension of the spring and mass of the rolls of loop forms oscillating chain with the small damping coefficient. Damping of the oscillating motion should be performed by using electronic control devices by introducing the signals of the change in velocity of the length of loop and its derivative into the control system or by using the mechanical dampers [1]. For this reason, additional devices and equipment are required. It is obvious, that the best rewinding system should be the system with the direct measurement of tension force of the band. Therefore, the stand is designed in this way and investigated in this work.

This work is organized as follows: the structure of the lab stand is presented in the second chapter. The development of mathematical model of the lab stand is presented in the third chapter. The results mathematical modeling and real measurements are presented in the fourth chapter. The conclusions are presented at the end of the article.

Structure of the lab stand for tight band coiling

The tight band coiling system is a variation of the classical structure of the web coiling. The designed lab stand exactly imitates industrial coiling process at reduced size. The path of the band movement on the stand might be observed in the Fig. 1. The braking torque of the unwinding roll 1 is controlled by electromagnetic friction clutch. The unwinding roll 1 (Fig. 1) reel is mounted on the LENZE electromagnetic braking clutch [11] of type 14.512 with 14.422 control unit 5 used for controlling the braking torque. The braking torque is adjusted by changing the current in the clutch windings trough the controllable rectifier 5 (Fig. 1).

The linear velocity of the band is controlled by the frequency converter with electrical drive EVS9322–ES 3, 4 (Fig. 1). The angular velocity of the roll 3 (Fig. 1) is stabilized by using the feedback signal of linear velocity of the band. The tension force of the band is measured by the deformation transducer on the freely moving roll 2 (Fig. 1). Deformations are transformed into the electrical signal, which are proportional to the tension force of the band.
Regulator PCTRL2 of tension of the band is implemented inside the frequency converter 4 (Fig. 1). The desired tension force of the band is passed to the controller through the connected computer. The feedback signal of the tension force is fed directly to the frequency converter. For the parameters observation and control the blocks with control devices 6) and measurements 7 (Fig. 1) are used.

**Functional diagram of the lab stand**

The functional diagram of the lab stand is presented in Fig. 2. The band is coiled from unwind roll UR on the roll WR. The control of the velocity of the tight band is done through the controller (control unit 3C) with feedback from transducer ST, reference unit HS through the frequency converter U1, and induction motor M.

![Diagram of the lab stand](image)

**Fig. 2.** Functional diagram of the lab stand

The tension force of the band is controlled by changing current \( i \) of the friction clutch FC winding. The elongation of the band is proportional to tension force \( F \) of the band. It is evident that signal of transducer FT measures the tension force of the band. So, the second closed loop regulates the tension force of the band and consists of the controller GC, transducer FT, reference unit HG, and converter U2.

**Development of the block diagram of the laboratory stand**

Functional diagram of the laboratory stand is shown in Fig. 2. As it was discussed previously, the tension force of the band depends on the friction clutch FC. The increased torque, developed by friction clutch, increases the tension force of the band. As a result the tight band will elongate. Process of band coiling might be illustrated by the simplified kinematical diagram (Fig. 3).

Investigated process of the tight band coiling is made by assuming that the band is elastic and has no weight [4].

In diagram: \( L \) is the length of the band for range \( B \) when the band is not tight (Fig. 3); \( l \) is elongation of band due to tension force. During the stabilized process, the amount of material coming into the range \( B \) equals to the amount of leaving material. That does not happen during transient response, because the tension force \( F \) and elongation \( l \) are being changed.

![Kinematical diagram of tight band coiling process](image)

**Fig. 3.** Kinematical diagram of tight band coiling process

Length of the band coming into range \( B \) is \( L_2 \) (winded-off length), and \( L_1 \) (winded-on length) is the length of band coming out of the range, recalculated to the length of the loose band. The elongation of the band due to tension force in the range \( B \) equals to:

\[
l = L_1 - L_2 + l_0, \tag{1}
\]

where \( l_0 \) – the initial elongation of the tight band, at the starting moment \( t=0 \) s.

The relative elongation is proportional to the tension force \( F \) and it equals to:

\[
\delta = ll/L. \tag{2}
\]

The speed of the moving loose band \( v_1 \) is obtained by multiplying speed of the moving tight band by the value \( \alpha < 1 \). For the band moving between the shafts it is possible to write the following system of the equations [4]:

\[
\begin{aligned}
\frac{dl}{dt} &= \alpha \cdot v_1; \\
\frac{dl}{dt} &= v_2; \\
l &= l_1 - L_2 + l_1; \\
\delta &= \frac{l}{l/L - l}; \\
F &= k_i \cdot \delta; \\
\alpha &= \frac{l}{l/L - l}.
\end{aligned}
\tag{3}
\]

Here \( D_{01} \) is the initial diameter of coiling bobbin; \( B \) is the thickness of the band; \( F \) is the tension force; \( v_1 \) is the linear speed of the coiling; \( v_2 \) is the linear speed of unwind unit.

The first, the fourth and the sixth equations of the system are nonlinear. Therefore the tight band system is nonlinear also. The dynamic of the friction clutch and unwind roll section can be described by set of differential and algebraic equations (4).

\[
\begin{aligned}
\frac{dl_1}{dt} &= \frac{U_s - R_s}{L_s} - i_s; \\
\frac{dl_2}{dt} &= \frac{1}{J} \cdot (M_F - M_s - M_i); \\
\frac{dl}{dt} &= \frac{b}{\pi} \cdot \omega_2; \\
\frac{d\omega_2}{dt} &= \frac{R_s}{J} \cdot (D_{m2} - d_2); \\
v_2 &= R_2 \cdot \omega_2; \\
M_F &= R_2 \cdot F; \\
M_s &= k_m \cdot i_s; \\
M_i &= k_i \cdot \omega_2; \\
M_a &= R_1 \cdot F; \\
M_u &= \frac{1}{l} \cdot M_u.
\end{aligned}
\tag{4}
\]

Here \( l_i \) is the excitation current of friction clutch, \( U_s \) is supply voltage of the clutch, \( L_s \) is inductance of the excitation winding of the clutch, \( R_s \) is the active resistance of the excitation winding of the clutch, \( d_2 \) is the decrease of diameter of unwind roll, \( b \) is the thickness of the band, \( \omega_2 \) – angular velocity of unwind roll, \( v_2 \) is the linear velocity of the unwinding band; \( D_{m2} \) is maximum diameter of unwind roll, \( R_1 \) and \( R_2 \) - corresponding radii of wind and unwind rolls, \( k_m \) is transferring coefficient of the clutch, \( M_F \) is the torque produced by tension force; \( M_s \) is the torque developed by the clutch, \( M_i \) – estimated friction torque of the unwind unit; \( k_i \) is the friction coefficient; \( F \) is the tension force of the band, \( M_u \) – loading torque of the
winder, \( J_i \) is the inertia of the unwinding roll, \( i \) – reduction coefficient of the gearing, \( M_{lo} \) is the load torque of the motor.

The first equation of this system in (Eq. 5) gives the dependency of the excitation current \( i \) of the friction clutch on the supply voltage \( U_s \). The second, third and fourth equations give us angular velocity of unwind roll \( \omega_2 \) decrease of diameter of unwind roll \( d_2 \), and radius of unwind roll \( R_2 \). The fifth equation – dependence of the linear speed \( v_2 \) of unwinding band on the angular velocity of unwind roll \( \omega_2 \) and radius of unwind roll \( R_2 \). The sixth equation - dependence of the torque \( M_F \) on the tension force \( F \) of the band and radius of unwind roll \( R_2 \). The seventh equation – dependence of the torque developed by clutch \( M_c \) on the excitation current \( i \). The ninth equation – dependence of the load torque \( M_\text{s} \) on the tension force of the band \( F \) and diameter of winding roll \( R_1 \).

The dynamics of the rewinding roll section have been composed by using structural schemes of coiling process [3] and mathematical description of dynamics of the tight band [4]. In such a way the block diagram of a whole system (Fig. 4) consist of two parts: winding unit (WU) and friction clutch unit (FCU).

![Fig. 4. Block diagram of automatic control system of the stand](image)

**Investigation of dynamics of the winding process**

The research of dynamics of coiling of the tight band has been done by using the mathematical modeling within MATLAB/SIMULINK. The step response of tension force on the band by using friction clutch has been investigated.

The curves (Fig. 5) shows good control quality of the tension force to the reference signal of tension force which appears ten second after the start. The system response to step of linear speed after 15 seconds is good enough but stabilization of the tension force appears with oscillations.

Similar experiments were performed with the real system, firstly giving step of linear speed and later step of tension force. For the measuring and registering the changes of linear speed and tension force the digital oscilloscope with two input channels were engaged. The scales of the signal measurement are: for measuring force 40 [N] per division and for measuring speed 0.2 [m/s] per division. During the first experiment values of the running coiling processes were as follows: tension force \( F=\text{const}=107.6 \) [N]; step of linear speed \( \nu \) from 0.3 to 0.6 [m/s] (Fig. 6a). The force \( F \) was slightly oscillated similarly to results of mathematical modeling (Fig. 5).

![Fig. 5. Simulated curves of the tight band winding](image)

In the second round of experiments the values of the running coiling processes were as follows: step of tension force \( F \) from 53.8 to 107.6 [N]; keeping the linear speed \( \nu=\text{const}=0.3 \) [m/s]. Good coincidence of experimental results with results obtained by mathematical modeling was observed (Fig. 6b).

**Conclusions**

1. The lab stand with real tide band coiling system was designed and compared with mathematical model. The stand is designed in the way to control the rewinding process with direct measurement of tension force. With this stand there exist several possibilities to demonstrate and investigate various conditions of coiling process for educational and scientific purposes.
2. The mathematical model has been developed to simulate the real stand for tide band coiling. Mathematical modeling allowed to investigate the dynamics of coiling system and to find the relationship between the tightness of the band, and the coiling speed.
3. The results of the mathematical modeling well coincide with the real experimental results. Therefore this model might be used for determining optimal PID controller parameters of the real time band coiling system.

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References


Processes of rewinding the tight bands of various elastic materials are very often in various technological lines. The highest process control quality is achieved only by employing feedback signal of tension force of the tight band. Therefore in this article there is proposed structure of control system and strategies for control with direct measurement of tension force in a rewinder system. The proposed control strategy allows stabilizing the tension force neglecting the change of diameters of the unwinding and rewinding rolls. The tension force of the tight band is controlled by using the electromagnetic friction clutch while the linear speed of cooling is adjusted by frequency drive. For the proposed system the performance evaluation and adjustment the equations of nonlinear control system with three closed loops are developed and modeled by using “MATLAB/SIMULINK” program package. The results of the mathematical modeling have shown good coincidence with the real experimental results. Therefore the mathematical model might be used for determining optimal PID control parameters of real time band coiling system. III. 6, bibl. 11 (in English, summaries in English, Russian and Lithuanian).


Многие технологические процессы протекают с применением перематывания различных материалов. При перематывании ленточных материалов наилучшие показатели регулирования можно получить, используя системы с непосредственным измерением силы натяжения ленты. В работе рассматривается система перематывания упрогой ленты, позволяющая производить перематывание с постоянной скоростью и постоянное силой натяжения ленты при изменении диаметров разматываемого и наматываемого рулонов. Сила натяжения регулируется при помощи порошковой муфты торможения. Скорость перематывания стабилизируется частотным асинхронным электроприводом. Для полученной трехконтурной нелинейной системы автоматического регулирования сделано математическое описание, на основе которой создана структурная схема и осуществлено математическое моделирование при помощи пакета МАТЛАБ/СИМУЛИНК. Результаты математического моделирования довольно точно совпадают с экспериментальными исследованиями. Созданная математическая модель может быть использована для оптимизации параметров ПИД-регулятора в реальной системе перематывания ленты. Ил. 6, библ. 11 (на английском языке; рефераты на английском, русском и литовском яз.).


Daugelyje įrenginių technologinis procesas vykdomas peryvinojant įvairias medžiagas. Geriausius reguliavimo rodiklius galima gauti naudojant tiesioginio juostos ūtėpmio jėgos matavimo sistemą. Darbe nagrinėjama lankočios juostos peryviniųjimo sistema, įgalinant peryviniot pastovų griečių palaikant vienodą ūtėpmimą keičiantis nusavyiojimu ir užvyvinojimu ritiniams skersmenims. Juostos ūtėpmio įjė naudojant tiekelinio stabdymo mūsų, o vyniokojo gretis stabilizuojamas asynchronine dažnimė elektros pavarų. Gautai trijų kontūrų netiesinė automatino reguliavimo sistemai surašytos pagrindinės matematinės priklausomybės ir jį pagrindu sudaryta struktūrinė schema bei atlikus matematinis modeliavimas naudojant MATLAB paketą. Matematinio modeliavimo rezultatai gana tiksliai sutampa su eksperimento rezultatais. Taigi sukurtas matematinis modelis gali būti panaudotas realios ūtėptomos juostos peryviniųjimo sistemos optimalaus PID reguliatoriaus parametrams nustatyti. II. 6, bibl. 11 (anglų kalba; santraukos lietuvių, anglų ir rusų k.).